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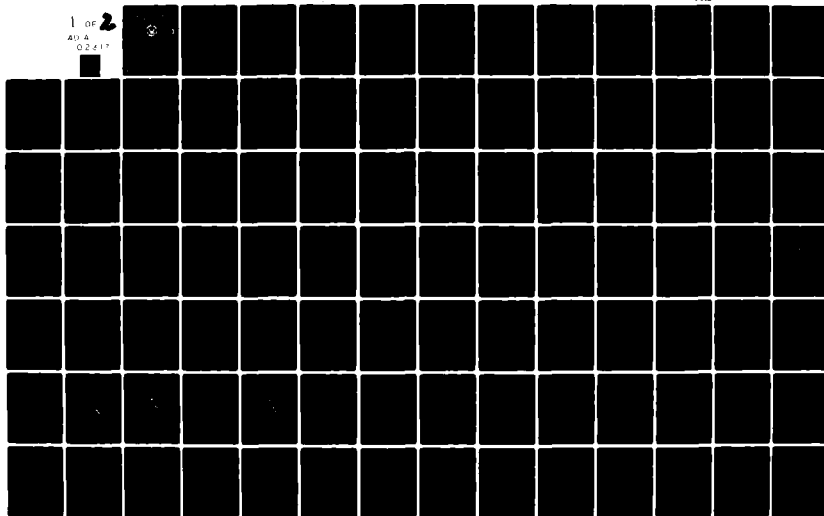
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THESIS

DYNAMIC ROUTE SELECTION
FOR LAND COMBAT SIMULATION MODEL

by

100 Posma R.M./Situmorang

11 Mar ~~1980~~ 1981 *12-1-81*

Thesis Advisor :

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Dynamic Route Selection for Land Combat Simulation Model

by

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Major, Indonesian Army
Ir., Institute of Technology, Bandung, 1966

Submitted in partial fulfillment of the
requirements for the degree of

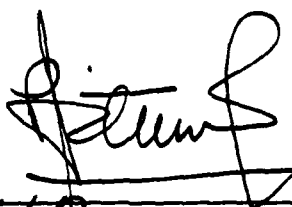
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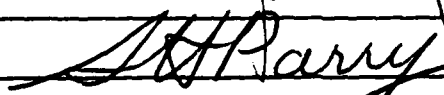
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March 1981


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ABSTRACT

This thesis presents a dynamic route selection model for the ground combat simulation environment. An optimal route is selected for an advancing combat unit, taking known enemy location(s) into consideration. The selected route is in the form suitable for a single vehicle movement.

The model is explained in detail, the complete listing is displayed and some results from exercising the model are presented and discussed.

The exercise was conducted on a digitized terrain, yet with simple modification it can work with functional terrain as well. The modification is explained, along with others that may be of interest to users.

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I. INTRODUCTION

Route selection in a ground combat environment is a very complex topic. In order to model it satisfactorily, one should not focus all the attention on the optimization aspect alone. Modeling the human decision making process with its (commonly occurring) failures to attain exact optimal solution is a more difficult task. Hence, a good route selection model should work within an optimization scheme, yet still possesses some level of uncertainty of attaining exact optimality.

Chapter II presents basic concepts in recognizing the problem in its naturally complex form. Then, in conjunction with the aforementioned consideration, some simplifications are performed. A number of approaches that have been taken in the past to model routing and route selection process are surveyed. The approach for this thesis is presented in the last sections of this chapter.

Optimization of the route is conducted in two stages. The first stage computes traveling cost for each small segment of route on the battle terrain. A great number of these optimizations build up a map of traveling costs on the region of interest. At this stage the influences of the defending force and terrain threat are taken into account. To represent the terrain a network grid of arcs and nodes

is used, such that the scheme becomes that of network programming and is presented in Chapter III. Further, Section III.B considers and selects the optimization algorithm to be employed: the Dijkstra Algorithm.

The network grid representation has a desirable quality that fulfills (at least partly) the need for uncertainties in the optimality of the selected route mentioned before. This is due to the sensitivity of the optimality to the size (or length) of segments used in the terrain representation.

Chapter IV provides the users with the descriptions of the logic used in the route selection routine. Each subroutine is discussed in detail.

Model exercise is a "must" in a model development task. Thus a sample terrain is created, digitized and used in the exercise. Two units of defending forces are considered and each is provided with its own influence map on the whole terrain. Chapter V presents these discussions, including the results of the exercise.

Even though a digitized terrain is being used in the exercise, one should not have the impression that a continuous terrain combat simulation cannot use this routine. Slight modification in SEGOPT-subroutine will enable this routine to be used in a simulation with continuous terrain representation. Section A of Chapter VI explains this, along with other modifications that might be of interest to users for other applications. The last section of Chapter VI deals with the problem of formation control of

the advancing unit in conjunction with the route selection problem. Conceptually the discussion leads to solutions which in the future can be realized, given sufficient time and resources.

II. THE ROUTE-SELECTION PROBLEM

A. NATURE OF THE PROBLEM

In the neighborhood of a village on a mountain, one could observe a large number of footpaths that were made by the villagers months or years before. Some of the paths may be straight and level while others may be climbing steeply or curving around the foot of a hill.

Obviously, all the paths manifest the (human) decision making processes that have taken place in the attempt to obtain routes which can be covered with the least effort. Thus, the notion of optimizing routes has been of concern to people even in the ancient times.

Taking one simple example of those paths, a route selection process is illustrated in Fig. II-1, and the problem can be stated as:

GIVEN : S, as the starting point; D as the destination;
both are located close to a hill (as illustrated).

DETERMINE: the optimal route (given some criteria of optimality).

Referring to Fig. II-1, most of the villagers would not choose path "c." It is too steep to climb and too much energy will be expended this way. Path "a" is also not desirable; it is too lengthy, curving around the foot of the hill. Again, too much effort will be spent traversing it. To most of the

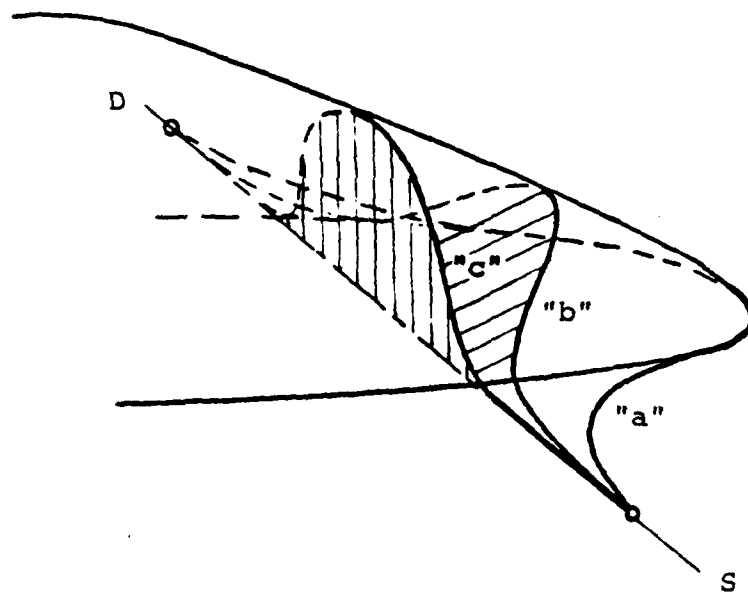


Fig. II.1. A Simple Hill with Routes to Select From.

villagers, path "b" (or another close to it) would be the most desirable solution.

An analyst would immediately start quantifying the parameters involved in the problem and state it as follows:

GIVEN : S's coordinates; D's coordinates; the Hill.

DETERMINE: an optimal path such that energy expenditure will be minimized.

The analyst will recognize the trade-off that exists in this situation as:

PATH GRADIENT vs. PATH LENGTH

and use this as the main consideration in obtaining the desired path.

Before proceeding further to obtain the solution, the analyst will also quantify the "trade-off" parameters:

1. Distance traveled (in meters);
2. Path gradient (in meters per meter of horizontal distance;

or alternatively:

1. (horizontal) Distance traversed, transformed into energy spent (in calories);
2. Path gradient in terms of potential energy, i.e., in calories necessary to cover the gradient per unit of (horizontal) distance traversed.

In this form the problem is workable and can be solved satisfactorily. Without further discussion it can be stated that the optimal path will be path "b" or another close to it.

It should be noted that sometimes one can observe conflicting solutions to the problem, i.e., in the form of "double-path;" paths that connect the same starting and destination point, running almost parallel to each other, yet on different elevations. This situation can be regarded as the manifestation of two things:

1. In conducting the trade-off, people tend to be influenced by preference, which is usually dominated by personal objectives;
2. In the real world, the optimal route is found only by coincidence. This is especially true in the situations where the paths are not prepared by people, which are situations generally found in combat.

Even though it was not presented explicitly, the author believes that Clark [Ref. 1], Kramer [Ref. 2], and Faulkner [Ref. 3] have considered similar trade-off schemes in working out their models (see Chapter II.C for further discussion). The main differences are in the quantification of the "trade-off" parameters and the algorithms being employed.

In this thesis the quantification will be done in the following manner:

- The starting and destination points are presented by the coordinates of each point in the coordinate system of the map used in the combat;

- The defending units are considered to create "hills" (of potential or threats) and the "steepness" is measured by the gradient of threat imposed on each moving element in the vicinity. This threat is further quantified by the probability of being killed ($P(\text{killed})$) by enemy weapon systems;
- The "distance traversed" cannot be suitably represented by distance in this case; otherwise there will be no conformity between the units of the "trade-off" parameters. In this route selection process the notion of "wear" will be used in place of distance traversed. It is obvious that "wear" is a function of both travel speed and distance traversed (note that a mountain climber also observes this parameter). Thus, to conform to the other trade-off parameter, "wear" will also be measured in terms of probability of being killed due to terrain (which is also a function of speed and covered distance).

Hence, in this quantification scheme, the "trade-off" parameters have identical unit of measure such that the problem can be worked out more easily.

B. PROBLEM DEFINITIONS

The problem of route selection for an advancing combat unit is very complex, both in a real combat situation and in a combat model environment. There are so many interacting

and influencing factors that it is impossible to list them all. A few of these factors are given below:

1. Speed of movement. This depends upon:
 - vehicle specifications,
 - terrain and weather conditions,
 - tactical situations.
2. Mode of movement, which can be categorized as:
 - approaching mode, i.e., when the advancing unit is still out of range of the defending weapon system;
 - attacking mode, when the unit is advancing closer to the defender's front line;
 - moving to a second (defensive) position;
 - infiltration mode;
 - (logistic) convoy.
3. Terrain conditions, with its characterizations:
 - passability (soil conditions, vegetation, etc.);
 - concealment, which determines detectability and also speed of movement;
 - texture; influences the speed of movement.
4. Known enemy units, their location and strength which impose threat upon the maneuvering unit.
5. Number of elements in the maneuvering unit and the formation being chosen can also be a dominant factor in the selection of a route.

If all those factors can be handled satisfactorily, this problem can be formulated as a multiple objective optimization problem:

GIVEN : - known enemy units (location/strength);
- terrain/weather conditions;
- advancing unit, elements and location;

DETERMINE : Route of movement and choose the formation, such that:

OBJECTIVES: a. Travel time is minimized;
b. Territorial gain is maximized.
c. Enemy casualties are maximized.
d. Friendly casualties are minimized.

The situation is worsened by the fact that the objectives are interactively influencing each other. It is obvious that at present this kind of problem cannot be handled satisfactorily in a modeling environment where limitations of resources should be recognized. Even in the real world where fewer limitations are observed, the "BLUE" and the "RED" forces should employ the doctrines as prescribed:

***Red would only advance its units if they overwhelmingly outnumber the BLUE elements. Further, maximum speed will be executed in order to minimize travel time and maximize territorial gain. Therefore, objectives a and b given above dominate, while the doctrine hopes that objectives c and d will follow suit.

***BLUE, on the other hand, relies on artillery support (plus close air support) rather than on the outnumbering factor. Hence, in this case the c and d objectives are the dominating ones.

Realizing this fact, it is considered justifiable to simplify the route selection problem and reformulate it into a more workable form. In this step measures have been taken such that most of the aforementioned factors are incorporated in the route selection process:

- GIVEN : 1. Known enemy locations and strength;
2. Terrain and weather conditions, passability and vehicle specifications, combined in a single parameter "Recommended Rate of Advance" for each small section of the battlefield;
3. Terrain vegetation and concealment (in terms of "concealment classification") at every location on the battlefield.¹
4. Probability of being killed ($P(\text{killed})$) by the defending force for each maneuvering element;

DETERMINE: The optimal route and the rate of advance of the movement.

¹In the routine, the inverse "openness-factor" is used.

SUCH THAT: At the defending force's front line, the maneuvering unit should still be as intact as possible (maximum number of elements survive the route selected).

The above formulation is capable of being modeled, yet it captures most of the factors that determine the route selection process in the real world. It should be noted that the choice of formation will not be explicitly considered in this model.

C. MODELING APPROACH

Various approaches have been used in modeling a route selection process. The DYN TACS MODEL [Ref. 1] views the route selection with the objective to minimize difficulty in traversing a route. "Difficulty" is defined by the travel time and exposure time to the enemy. DYN TACS employs a Dynamic Programming technique (for shortest path) to determine the optimal route for an advancing unit within a "patch" of the terrain.² Moving this "patch" toward the objective and performing the optimization sequentially leads to a desired result. However, this can only guarantee locally optimum segments which do not necessarily add up to a globally optimum route [Ref 1].

²No specific algorithm has been mentioned explicitly in the report.

Kramer [Ref. 2] also developed a model to obtain the optimal route for an advancing unit. With the same trade-off technique as that used in DYN-TACS, Kramer uses the Dijkstra Algorithm. Again, the route selection is done sequentially, from the starting point (through a predetermined horizon) to the destination by moving the optimization network along the route.

A globally optimum solution was worked out by Faulkner [Ref. 3] for submarine routing. The problem's objective is to minimize the probability of being detected for a submarine by known or suspected enemy sensors' locations. With various influencing factors such as current, depth and length of time of submergence, the Variational (Calculus) Technique was used, yielding a globally optimum route.

Initially the author considered the use of the Calculus of Variation Technique in the Land Combat environment, but the elaboration and the demands on computer resources were prohibitive. Moreover, it should be realized that in Combat Modeling environment the optimality of the solution is not the only objective. More important than that is the attempt to model the human decision making involved in the selection of routes, which employs neither a computer nor the Calculus of Variations. Clark [Ref. 2] has discussed the human decision making topic in the DYN-TACS Reports.

With the above discussion, supported by some other considerations presented in Chapter III, it was finally decided

that Dijkstra Algorithm is selected to be used in this model.

D. COST FUNCTION AND OUTPUT VARIABLES

With the problem formulation as presented in Section II.B, it is necessary to define the cost-function and output variables for the optimization routine to work with. The following observation came from the real world:

A commander of a maneuvering unit may find it difficult to bring accurate firepower to bear while enroute to the objective (destination). In a rugged terrain, with vehicles lacking perfect shock absorbing devices, it is very difficult for the firer to aim and accurately fire on the enemy elements.³

Therefore, it may be desirable to advance the unit as fast as possible, but it is important to keep the losses to a minimum such that in the close-in phase of the combat, the attacker could substantially outnumber the defending elements in order to realize success.

This view is believed to be true for both tanks and infantry units as well. Therefore, the cost function of the route selection process is to minimize the probability of being attrited enroute to the destination.

³This is realized by both "RED" and "BLUE" military scholars, which leads to those aforementioned doctrines.

The cost function, i.e., the probability of being attrited ($P(\text{killed})$) comes from two sources:

1. The enemy elements, usually located in the vicinity of the destination point of the route, as well as those located along the way (outpost, ambush, etc.).
2. The terrain. One may argue that attrition due to terrain occurs infrequently. It is included in this model since in the real world (although subconsciously) it is also considered by the driver or the unit commander. One can observe that a driver will drive his vehicle only as fast as his "safety-consciousness" permits, i.e., by slowing down whenever the route becomes very rough, by avoiding rocks, tree trunks, ditches or other obstacles, and occasionally by violating the formation or speed dictated by the unit commander.

The above observation leads to the trade-off scheme used in this model.

$P(\text{KILLED})$ DUE TO ENEMY vs. $P(\text{KILLED})$ DUE TO TERRAIN
which is analogous to the trade-off scheme discussed in Section II.A.

It is apparent that increasing the speed of movement may reduce $P(\text{killed})$ due to enemy's weapon, but it also increases $P(\text{killed})$ due to terrain and overspeeding; thus rate of advance will be an equally important output variable as the route itself.

In a combat model a terrain-killed vehicle may be considered to be mobility killed. In the case of an advancing unit, it can be considered as being K-killed (Catastrophic-killed), since it cannot participate in the "close-in" battle later on. Because of the chance of killing friendly elements, the terrain-killed vehicle could not even give fire support to its unit during this phase of the combat. This observation allows the model to pool the probability of being (mobility) killed by the terrain into the same category as the probability of being attrited by enemy elements to obtain a total $P(\text{killed})$ (assume additivity) enroute to the destination. This total $P(\text{killed})$ will be used as the cost function for the optimization problem.

In the subsequent sections, a number of hypotheses will be presented. These include the functional relationship between the probability of being killed ($P(\text{killed})$) due to enemy as a function of speed and distance, and also $P(\text{killed})$ due to mechanical failures. It is important to bear in mind that those hypotheses are presented to clarify the model and to provide a data base for model exercise. The model itself has been designed so as to be independent of those hypotheses. Therefore, whenever different relationships are obtained and are used with the model, the output will be equally valid.

E. RECOMMENDED RATE OF ADVANCE

In traversing a particular area on the terrain, a driver continuously adjusts the speed and direction of the vehicle in accordance with the terrain conditions (soils, shrubs, rocks, ditches, etc.), the vehicle capability (specifications), and the controllability of the vehicle (including the driver's ability) in order to avoid two kinds of accidents:

1. Mechanical failure, which will happen earlier with the increase of speed;
2. Loss of control (overturned, stuck in mud, mechanical failure due to collision, etc.).

The first category, in mechanical engineering terms is usually formulated as:

$$L|_{os} = L|_n \times (RS/OS)^P \quad (F.II-1)$$

where:

$L|_n$ = Life expectancy (in appropriate unit with normal usage (in accordance with recommended speed, etc.);

$L|_{os}$ = Life expectancy with overspeeding;

RS = Recommended speed (in appropriate speed units);

OS = Operating speed (in appropriate speed units);

P = Power factor, a constant for a given set of conditions.

For example, an overspeeding factor of 2.0 with a power factor of 3.0 might reduce the life expectancy to only 1/8 of normal.

In terms of probabilities, this formula can be presented as:

$$P_{\text{killed}}|_{\text{overspeed}} = (P_{\text{killed}}|_{\text{normal}}) \times (\text{OSF})^m \quad (\text{F.II-2})$$

where OSF is the overspeeding factor or the ratio between operating speed to the normal (recommended) speed.

For vehicles operating on rugged terrain, slowing down does not necessarily lead to the extension of vehicle life. Therefore, for operating speeds of less than the recommended speed, the speed ratio (RS/OS) or (OSF) still has the value of 1.0.

The "m" in (F.II-2), similar to "p" in (F.II-1), is a constant for a given set of conditions. This factor determines how progressively P(killed) changes as a function of overspeeding factor.⁴

The second category is more difficult to handle; no study has been found in this area. The occurrence of loss of control of vehicles is a complex subject of human factor engineering, and also involves synergistic effects which act on the driver (speed, vibrations, anxiety, stress due to the battle, etc.). Only intuitively can it be hypothesized that the probability of this kind of accident to occur is also a progressively increasing function of speed, such that it can

⁴In mechanical engineering environment the values of p is ranging from 1.0 to 4.0.

be pooled together with the first category as given in Equation F.II-2.

It is necessary to determine the values of two variables before continuing with the optimization problem:

1. $(P(\text{killed}) | \text{normal operation})$ or PKVL which, with engineering considerations, in the exercising of this model is assumed to be 0.0002 per mile traversed;⁵
2. Recommended rate of advance at any given location, defined as the smaller of the following:
 - a. The speed at which the driver can perform his task without excessive stress, (i.e., can perform safely and satisfactorily);
 - b. The speed at which there is no excessive stress imposed on the vehicle due to terrain conditions (and speed) which could lead to mechanical breakdown.⁶

Given those values, the relationship between $(P(\text{killed}) | \text{overspeed})$ and OSF will be in the form of a horizontal line (up to OSF=1.0, see discussion in the previous page), followed

⁵This value reflects the value of expected "trouble-free service" of a vehicle. It is measured in mile traversed in continuous service, without maintenance, before mechanical breakdown occurs. For example, a value of expected trouble-free service = 5000 miles can be regarded as PKVL=0.0002.

⁶These speeds are described by a map that gives values of safe rate of advance such that normal life expectancy is maintained. In its preparatory efforts, the recommended rate of advance is comparable to "SPEED.LIMIT" being used in the STAR-Model [Ref. 4].

by an increasing function as presented in Fig. II-2, given for a power factor value of 3.0.

F. PROBABILITY OF BEING KILLED DUE TO ENEMY (PKFOE)

The measure of probability of being killed by enemy elements used in the model is the value of $P(\text{killed})$ based on a time period equal to that of the firing cycle (FCYCLE) of the enemy weapon system. For "RED" tanks, firing cycle is usually in the range of 6 to 8 rounds per minute; for "BLUE" tanks it is about 3 rounds per minute. In exercising the model, a value of 20 seconds for FCYCLE is considered reasonable (assume BLUE defends).

Two major factors that influence $P(\text{killed})$ by the enemy are crossing speed and distance to the enemy element. Each will be discussed below.

1. $P(\text{killed})$ as a Function of Speed

The degradation of $P(\text{killed})$ with increasing crossing-speed is caused by:

- increased aiming error, and
- lack of capability of the gun to follow the movement of the target (e.g., the case of a tank gun trying to shoot at a straffing aircraft).

Crossing speed is usually defined as the component of vehicle speed which is perpendicular to the firer-target line. In addition to this, the route selection model recognizes also the crossing speed in the sense of the component

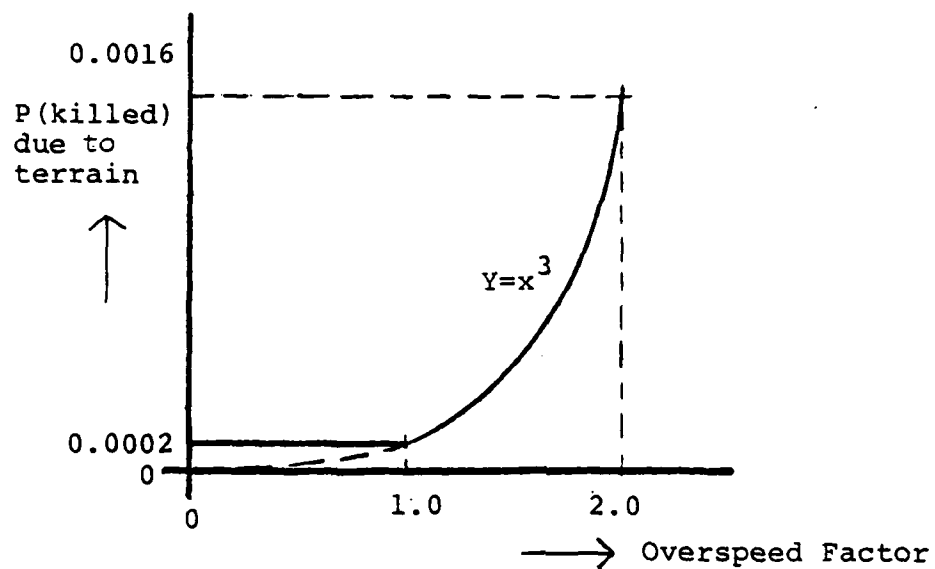


Fig. II-2. Pkilled due Terrain as a Function of Overspeed Factor

of vehicle speed which is perpendicular to the path of the incoming projectile. This occurs due to the nonlinearity of the projectile's path beside the non-negligibility of the vehicle speed as compared to the projectile's speed (Fig. II-3). Therefore, a moving vehicle can still create "miss distance" to the point of impact, even though the vehicle is moving in a straight line toward the firer. In other words, "some" crossing velocity may exist, even though the crossing velocity is zero relative to the firer. With the two "crossing speeds" acting together, the model may disregard the vehicle movements direction in applying the functional relationship, hypothesized as an exponentially decaying function (Fig. II-4a):

$$PKFOE|d = C_d \times \exp(-V) \quad (F.II-3)$$

where

PKFOE|d = probability of being killed by defending
(enemy) unit at range, D.

C_d = range dependent coefficient, 1.0 at D=0.0;

V = crossing velocity of the vehicle measured
in appropriate units.

2. P(killed) as a Function of Distance

The decaying of PKFOE with the increase of distance can be treated similar to the decaying of P(detected) with increasing distance. With this similarity, PKFOE can then be represented by another exponentially decaying function (Fig. II-4b):

$$PKFOE|v = C_v \times \exp(-D) \quad (F.II-4)$$

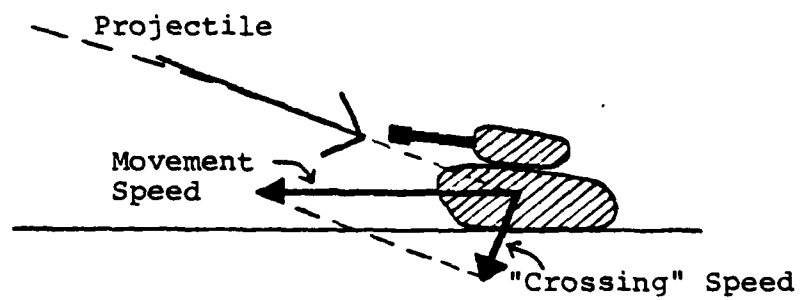


Fig. II-3. Crossing Speed of a Vehicle From the Projectile's Standpoint

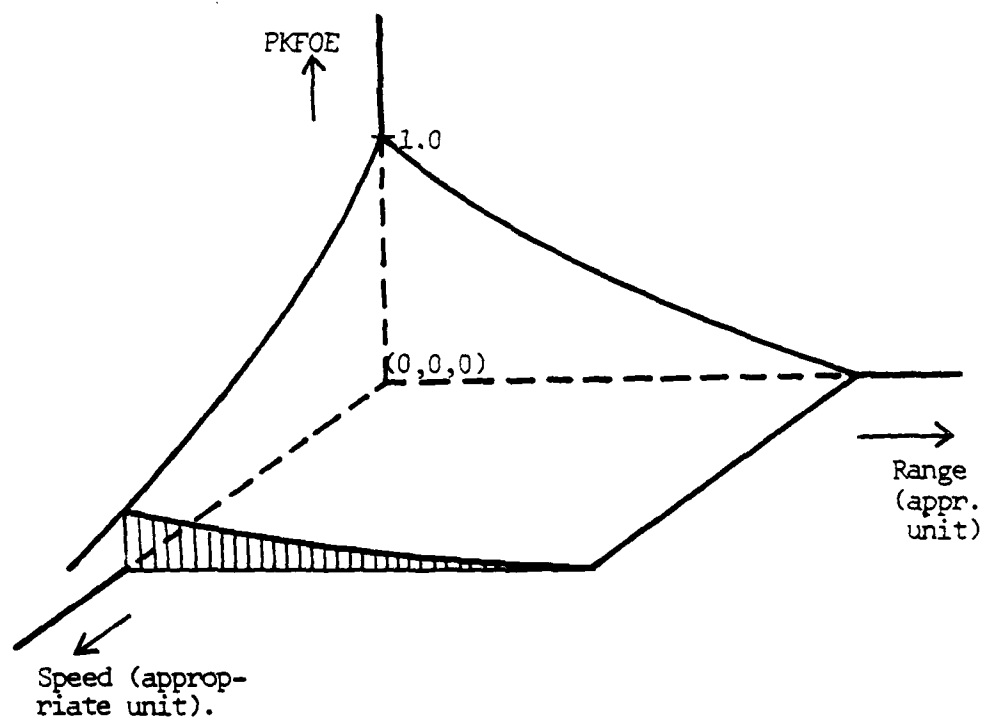
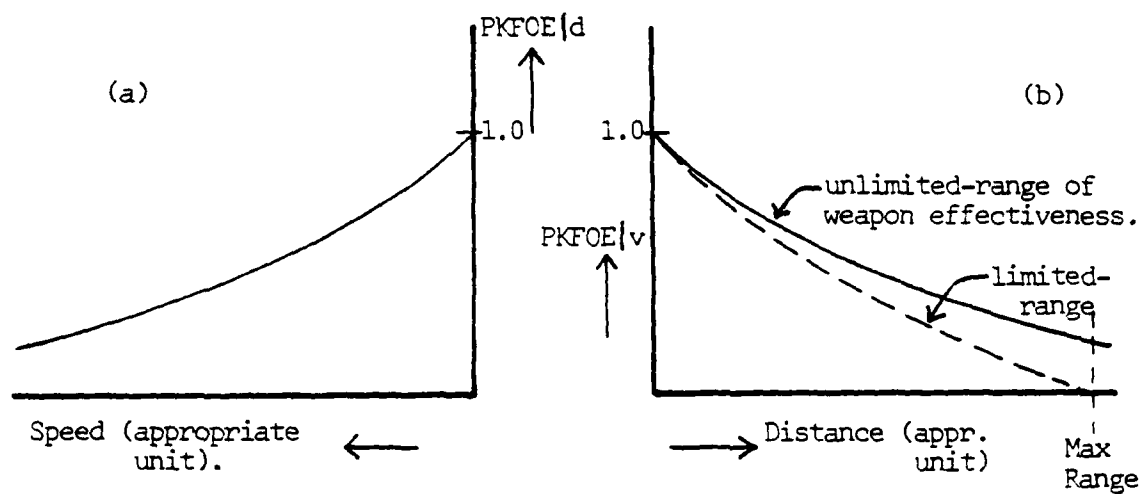


Fig. II-4. PKFOE as a Function of Range and Speed (Other factors are kept constant).

where:

$PKFOE|v$ = P(killed) by defending elements while
moving at speed of V (appropriate unit);

C_v = Speed-dependent coefficient, a constant
for a given crossing speed and decaying
with increasing speed, 1.0 at $V=0.0$;

D = Distance from the threatening enemy loca-
tion, measured in an appropriate unit.

3. PKFOE as a Function of Speed and Distance

It can be hypothesized now that PKFOE, SPEED and
DISTANCE become a three-variable function that can be
represented by (Fig. II-4c):

$$PKFOE = P_{0,0} \times \exp(-V) \times \exp(-D) \quad (F.II-5a)$$

or

$$PKFOE = \exp(-V) \times \exp(-D) \quad (F.II-5b)$$

where:

$P_{0,0}$ = probability of being killed by enemy element
while moving at speed = 0.0 at range = 0.0,
to which a value of 1.0 can be assigned;

V, D = speed and range, measured in appropriate units,
with the assumptions:

- detection has occurred before,
- defenders may fire at detected attacking
elements.

It is fully realized that in real world, PKFOE depends
upon more factors than the two described above. Again, it

will be emphasized that these hypotheses were formulated for the purpose of explaining the model. In the routine itself, the model does not perform functional computations for PKFOE values. Rather, a look-up table has been constructed. At present, the look-up table is based on the functional relationship:

$$\text{PKFOE} = \exp(-D) \times \exp(-V \times 2.25/60.) \quad (\text{F.II-6})$$

where all the variables are as previously defined. In this formula, the units being used are miles for the distance and meter per second for speed.

In the routine the value of PKFOE is set to zero for a distance equal to max. weapon range (4000 meters or about 2.5 miles). Whenever the model is used in a combat simulation, it is recommended that a more accurate look-up table be prepared in order to obtain more realistic results.

The hypothetical functional relationship is geometrically illustrated in Fig. II-4c, while the look-up table used in the exercise is presented in Appendix C (last array).

III. THE OPTIMIZATION STAGES

There will be two stages of optimization in this route selection model. The first stage, a small scale (within-route segment) optimization has the following formulation:

GIVEN : * maneuvering unit's location;
 * known defending units' locations;
 * next location (end-of-segment) of the
 maneuvering unit;

CONSIDER : * recommended rate of advance in the
 neighborhood;
 * concealment factors;
 * enemy influences;

OBJECTIVE: Minimize total $P(\text{killed})$, i.e., sum of $PKFOE$
 (due to enemy) and $PKVEL$ (due to terrain and
 excessive speed);

OUTPUT : Optimum speed and traveling cost in that
 particular segment.

If this optimization is performed iteratively for the whole region of interest, a discrete map of traveling cost will be obtained. The cost will be in terms of $P(\text{killed})$ for each advancing element in each (small) section of the map.

The second stage is the determination of the optimal route based on the traveling cost map obtained from the first

stage optimization, i.e., a route with the smallest cost ($P(\text{killed})$). This brings the model to the family of the shortest path algorithms.

The unsuitability of using Calculus of Variations in this modeling scheme has been discussed previously. Two choices remain, namely Dynamic Programming and Network Programming.

At this point it is important to consider how a unit commander selects a route in accomplishing his unit's mission. Having studied the topographic map carefully, a unit commander will first assess the possibility of moving his unit along some easily traversed route to the destination point. This is modeled by the consideration of MAPRSP, the map of recommended rate of advance. In addition, the unit commander will consider how the known enemy elements might threaten his unit's safety while traversing along each possible route. At this stage he may have discarded some preselected routes or modify the routes by changing direction for some of the segments to obtain a satisfying one.

Considering the terrain conditions he will also determine a reasonable traveling speed (not necessarily the maximum speed) to prevent separation between elements along the route. In addition, he has also considered the safety of each element due to terrain threat, since he has the

objective of reaching the assault line (enemy front line) with the maximum number of survivors.⁷

Later in the move, the route might be adjusted, either because of his unit's losses or new information about enemy locations or other tactical situations.⁸ At this point he might want to change direction, change speed or even go into hasty defense.

Several points are noted from the above observation:

- a. The selection of a route is usually done once for the whole path from the starting point to the destination (which may be either a temporary or intermediate destination);
- b. In the real world, the optimal route is only obtained by coincidence;⁹
- c. Adjustments might be performed along the route, but still adhere to the process described in a above;

⁷In this model, those considerations are not done in exact sequence as described; they are accomplished simultaneously.

⁸In a combat model, it is the second (or third, etc.) calling of the route-selection routine.

⁹Since the size of the segments in the Network terrain representation is not infinitesimally small, optimality is not guaranteed all the time. In Decision Theory [Ref. 1, pp. 5-11] the selected route is a "satisfying" one. Only in well behaved situations (thus coincidentally), will the route be optimal.

- d. In the selection of a route, the optimization is performed with "threat" in mind, firstly due to terrain, secondly due to enemy.¹⁰

Hence, the objective function can properly be stated in terms of threat ($P(\text{killed})$ or $P(\text{survive})$).

Based on the above discussion the optimization developed in this model will fulfill points a and d above. To fulfill point c, the routine is provided with various utility sub-routines in order to enable it to compute the optimal route with any starting and destination point input.

Point a above also implies that it is not necessary to model the route selection as a sequential decision process (namely Dynamic Programming); a simpler Network Programming algorithm will yield equally good results.¹¹

References 5, 6, and 7 claim that for the kind of problem encountered by this model (shortest path between a given pair of nodes), the Dijkstra Algorithm is still the most efficient one. It was, therefore, decided to employ this algorithm in the route selection optimization being worked in this thesis.

¹⁰Even if it is "consciously" stated as driving and riding comfort, it also reflects the safeguarding against attrition due to terrain.

¹¹Some authors classify Dijkstra Algorithm into the Dynamic Programming class of algorithms, and for "shortest path between a pair of nodes" problem, this algorithm is equally efficient as its Dynamic Programming counterpart [Ref. 5, pp. 54-58].

A. OPTIMIZATION WITHIN ROUTE SEGMENT

The scheme for the optimization is simply illustrated in Fig. III-1. In the computation the values of PKFOE are obtained from the PKFOE table (input data) which was prepared before the implementation of the model (see Chapter II). These values (one for each value of "rate of advance" being considered) are then entered into the following formula:

$$PKVOE = \sum_{I=1}^N \frac{PKFOE(IV,ID) \times \text{linf} \times \text{OPNF} \times \text{NDEFDK}(I) \times \text{ANGLFC}}{\text{NELATK}}$$

(F.III-1)

where:

- PKVOE = probability of being killed experienced by each attacking element within each time interval of FCYCLE-seconds for a given value of "rate of advance" of the maneuvering unit;
- PKFOE(IV,ID) = probability of being killed by I-th enemy element (unit) while having a rate of advance index, IV, at a distance index, ID, obtain from the look-up table;
- linf = a switching value, 1.0 if the segment is under influence of the enemy unit (element); 0.0 otherwise.
- OPNF = openness-factor, a value ranging from 0 to 10 (x10%); that is the openness of the terrain in which the segment of interest

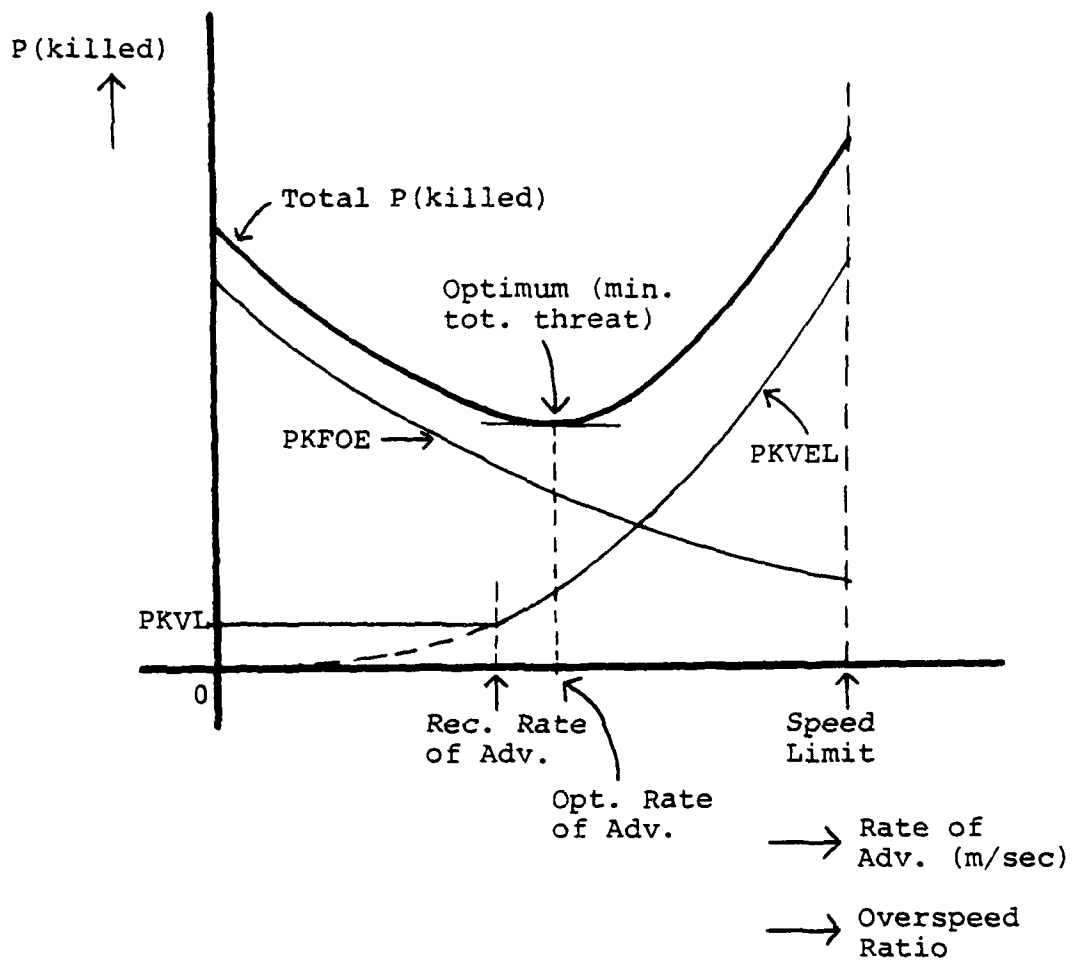


Fig. III-1. Optimization within Route Segment.

lies. This factor affects probability of being detected which further affects $P(\text{killed})$.

NDEFDK(I) = known number of enemy elements in I-th enemy unit.

NELATK = number of elements currently in the maneuvering unit (assumed uniform distribution of $P(\text{killed})$ among the elements).

ANGLFC = Aspect Angle factor, 3.0 for angles larger than 30 degrees, 1.0 otherwise;

N = number of known enemy units.

The value of PKVOE is computed for various values of rate of advance of the maneuvering unit. In addition, the routine computes the values of PKVEL (for the values of rate-of-advance) using the hypothesized formula (F.II-2). This value (PKVEL) is experienced by every maneuvering element.

Assuming additivity, PKVOE and PKVEL are summed to obtain PKTOT. After selecting the smallest value of PKTOT, the corresponding optimum rate of advance is transferred to the main routine (the Dijkstra stage).

B. THE ROUTE SELECTION

After performing many iterations of the "within segment" optimization, a map of point-to-point traveling cost is now obtained, analogous to the node-to-node costs encountered in a network programming optimization. A sample section of

that map is presented in Fig. III-2 where each arc has its own cost in terms of $P(\text{killed})$.

The correct statement for the objective function of this optimization problem is to maximize the probability of survival enroute to the destination. Thus, the cost must be expressed in terms of $P(\text{survive})$. The corresponding sample section is illustrated in Fig. III-3.

In computing the total probability of survival along the route from those $P(\text{survive})$ in each segment, multiplication is performed. Therefore, to enable the routine to handle the optimization by addition, the logarithmic value of each cost element is computed beforehand. In this log space, the addition of "cost" elements can then be performed, just as ordinary network programming does.

Further observation shows that:

$$\log (P(\text{survive})) = \log (1-P(\text{killed})),$$

which is approximately equal to $P(\text{killed})$ for small values of $P(\text{killed})$.

Table III-1 compares $P(\text{killed})$ with $\log(P(\text{survive}))$ for a region of small values of $P(\text{killed})$. Only nonsignificance differences are observed in that region. This approximation is used in the exercises described in Chapter V, but may not be appropriate when implemented in a combat simulation.

As previously described, the Dijkstra Algorithm was selected for the model. This algorithm is widely discussed

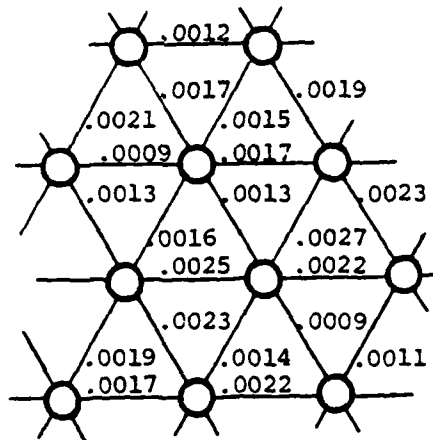


Fig. III-2. A Sample Section of the Grid with Cost Value Network (P(killed)).

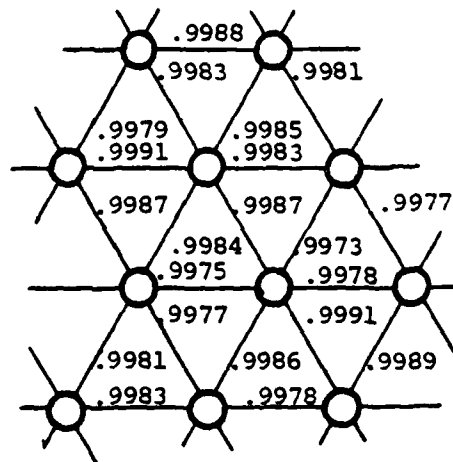


Fig. III-3. Corresponding Values of P(survive) with those of P(killed) in Fig.III-2.

TABLE III-1

COMPARISON BETWEEN P(KILLED) AND LOG (P(SURVIVE))

P(killed)	Log (P(survive) = log (1-P(killed))	% Difference in Abs. Values
0.1	-0.105	5.4
0.05	-0.05129	2.6
0.01	-0.0100503	.5
0.005	-0.005012	0.25
0.001	-0.0010005	0.05
0.0005	-0.00050001	0.025

NOTE: P(killed) for each segment traversed are very small values. It would not exceed 0.1.

in standard textbooks, and will not be discussed in detail in this thesis.

A way of saving in computational effort is mentioned in Ref. 1, which is employed in this model. The "within-segment" optimizations are not performed all at once to cover the whole terrain of interest. It is performed only when needed, (i.e., when, in the Dijkstra stage, a new node has just been permanently labeled and the cost values for the arcs adjacent to that node are being computed). Only at those times are the "within-segment" optimizations performed. In this way, the optimal route can be determined without "covering" the whole network grid with the optimized values of segment costs.

IV. THE ROUTE SELECTION ROUTINE

A. LOGIC STRUCTURE

Fig. IV-1 shows a flowchart outlining the logic used in the route selection routine. After reading the input data, a network of nodes and arcs is generated in accordance with the distance from the starting point to the destination and to the segment desired. The smaller the segment, the closer the result to the globally optimum route.

This network is then oriented with the actual starting and destination points on the topographic map. Topographic map coordinates corresponding to the node number of the network grid are then computed and tabulated in arrays: TOPOG(NNODE,1) for the abscissa (x-direction) and TOPOG(NNODE,2) for the ordinates (y-direction).

Comparing these values with the boundary values of the topographic map, the routine is then able to discard the outliers, i.e., nodes that fall out of the boundaries of the topographic map.¹²

The routine enters the Dijkstra stages and the enumeration of nodes is initiated from the destination node moving backward "toward" the starting node. During this enumeration,

¹²Or the boundaries of the sector of the maneuvering unit, if the combat simulation defines boundaries in that manner.

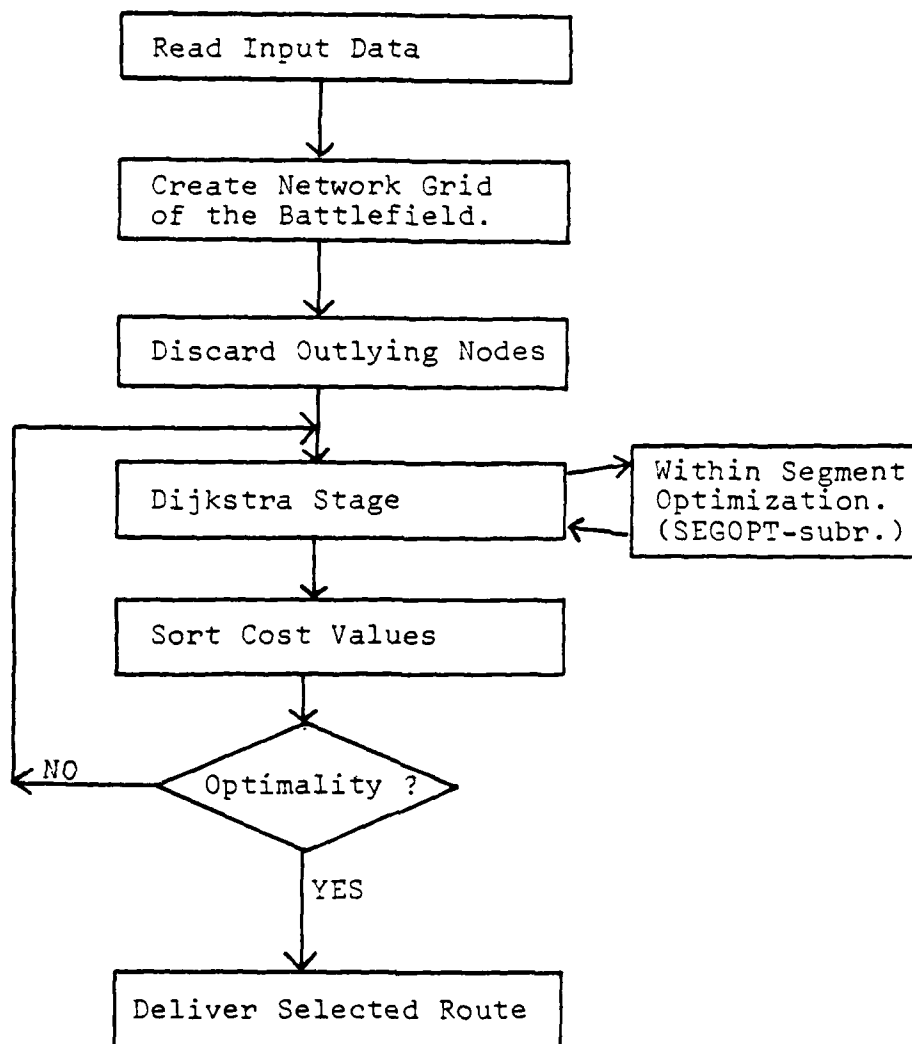


Fig. IV-1. Logic-Structure of the Route Selection Routine.

it is necessary to optimize the cost for each arc adjacent to the node being enumerated by calling the SEGOPT subroutine.

After each enumeration, a sorting routine is employed to find the least cost in the enumerated network, thus finding the next node to be processed. If this "next node" is identical to the starting node, an optimal route has been obtained. Using the predecessor array (LABLFP), the selected route can be "traced back" toward the destination node, and the route is then transferred to the (calling) combat simulation program in a form of array of topographic coordinates, i.e., in the form usable by the combat simulation.

A detailed description of the interface between the Dijkstra stage and SEGOPT subroutine is illustrated in Fig. IV-2. Fig. IV-3 is presented for clarification of the SEGOPT subroutine. Based upon Equation F.III-1, the logic is quite straightforward and the optimum rate of advance is obtained through sorting.

B. NETWORK REPRESENTATION OF THE BATTLEFIELD

For the route selection process, the battlefield or any region of interest of the battlefield is discretized into a node and arc network which is defined by the routine in lines 64 through 132 (Appendix B).¹³ A small sample section

¹³This routine is developed with a concept of a "moving template," i.e., the starting and destination point can be anywhere in the battlefield.

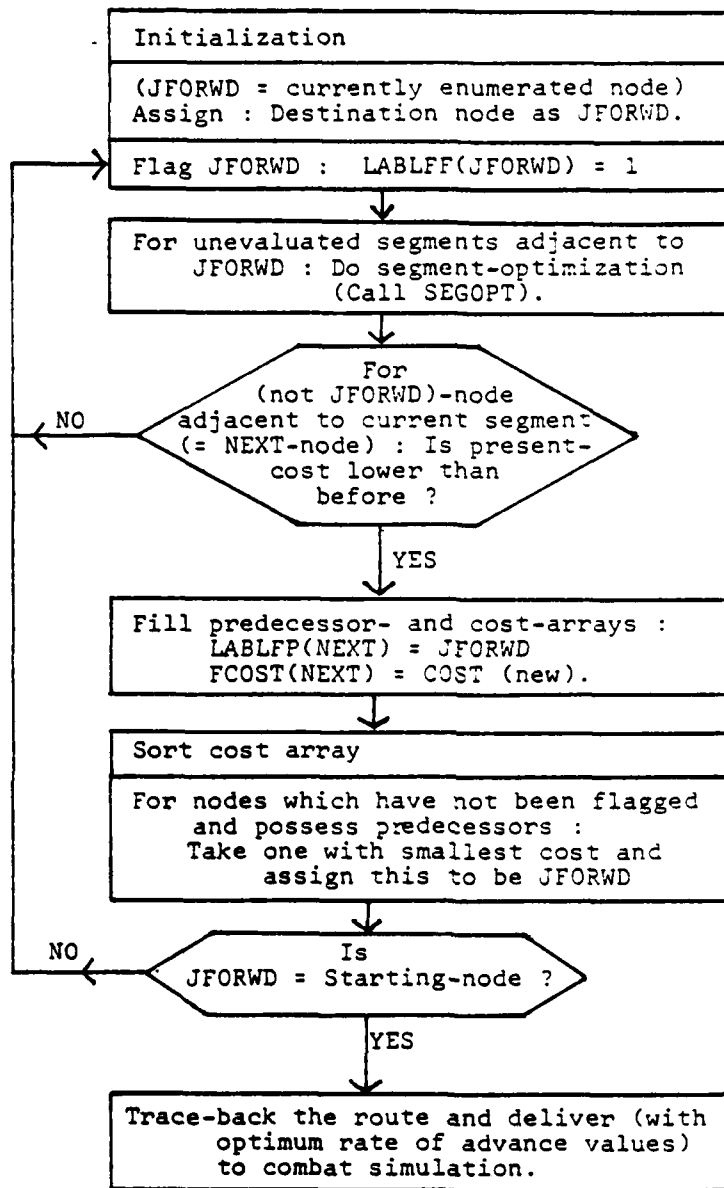


Fig. IV-2. Dijkstra Algorithm; Interaction with SEGOPT subroutine.

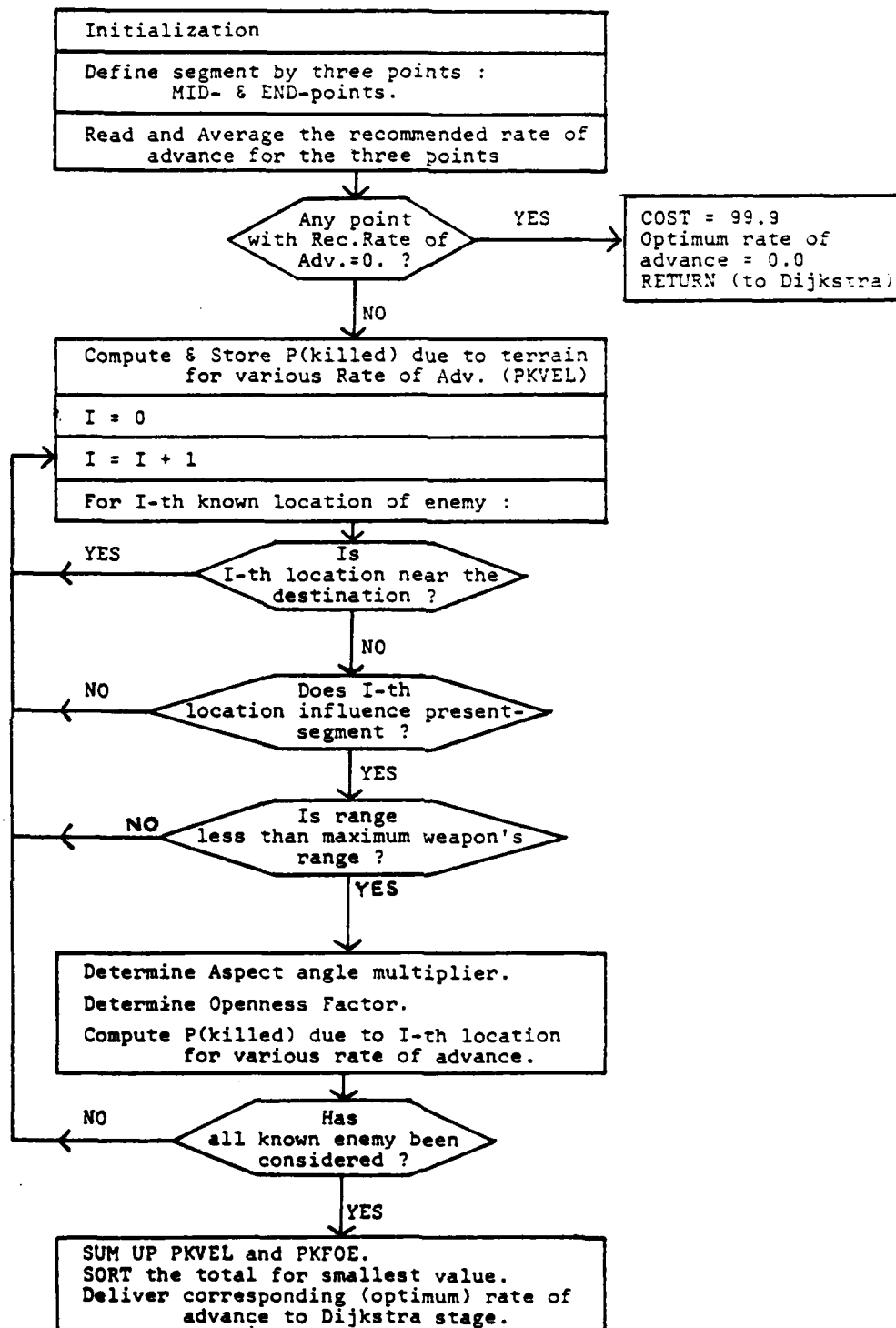


Fig. IV-3. Within-segment Optimization (SEGOPT-subroutine).

of the network is illustrated in Fig. IV-4 and the nomenclature is also presented.

The coverage of the network is defined in such a way that the maneuvering unit has ample space to choose its route. That includes the possibility of moving backward, circling around from the right or the left hand side of the terrain and even the possibility of approaching the destination point from the rear (see Fig. IV-5).

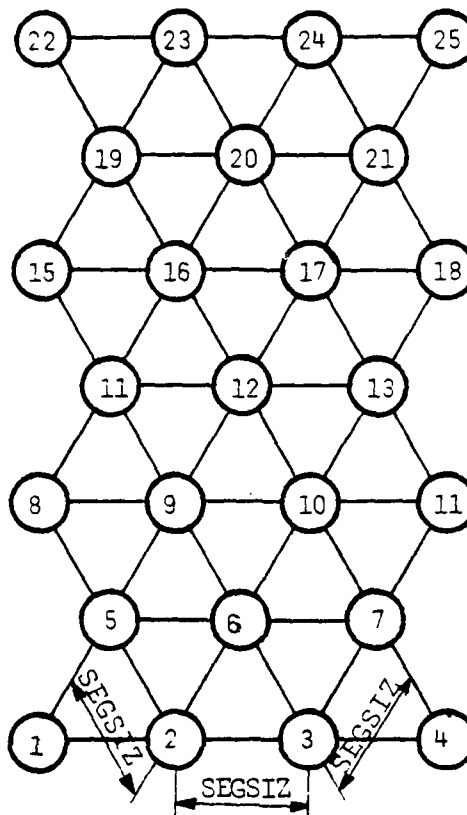
In the representation, node #1 is always located at the origin of an orthogonal route selection map. On this route selection map the network grid is overlaid. With this arrangement a node can be presented either by a node number or by a pair of orthogonal coordinates which is in a translated and rotated state with respect to the topographic map. Utility routines are required to handle the transformations among those coordinate systems.

It is apparent that the output of the Dijkstra Algorithm, which will be in terms of node number, should be transformed into orthogonal coordinates of the route selection map (the "moving template") and further transformed into the topographic coordinates which the combat simulation can use.

To summarize, the routine has to work with three different maps:

- a. The node and arc network, overlaid on
- b. The orthogonal coordinate system which moves whenever the route selection routine is called for route adjustment (R-S-Map);

$NCOLHX = 4$
 $NC1 = 3$
 $NCC1 = NCOLHX + NC1$
 $= 7$
 $NROWHX = 7$



NOMENCLATURE :

$NCOLHX$ = # nodes in the baseline of the network grid
 = # nodes in each odd-numbered row.
 $NC1$ = # nodes in each even-numbered row.
 $NROWHX$ = # rows of nodes in the network.
 $NTEMP$ = integerized value of distance divided by
 (SEGMEN \times SQRT3).
 $SEGSIZ$ = Working segment length (not necessarily equals
 to SEGMEN)
 = distance divided by $NTEMP$.

Example : If node-20 is the destination and node-6 the
 starting node, then $NTEMP = 2$.

Fig. IV-4. Network Representation of the Terrain; Nomenclature.

- c. The topographic map on which the other two are overlaid, which is the working map of the combat simulation program.

As an example, node #10 in Fig. IV-4 can be represented by location (2xSEGSIZ;SEGRT3) on the R-S-Map, where:

SEGSIZ = working length of route segment (not necessarily equal to SEGMEN, the user's input);

SEGRT3 = SEGSIZ x SQRT (3.0).

The utility routines are as follows:

1. OGXFNN;
2. NNXFOG;
3. RSTRTP;
4. TPTRRS.

The routine names use the following conventions:

NN stands for Node Number;

XF stands for transformed into;

OG stands for Orthogonal (coordinate system);

RS stands for Route Selection (map);

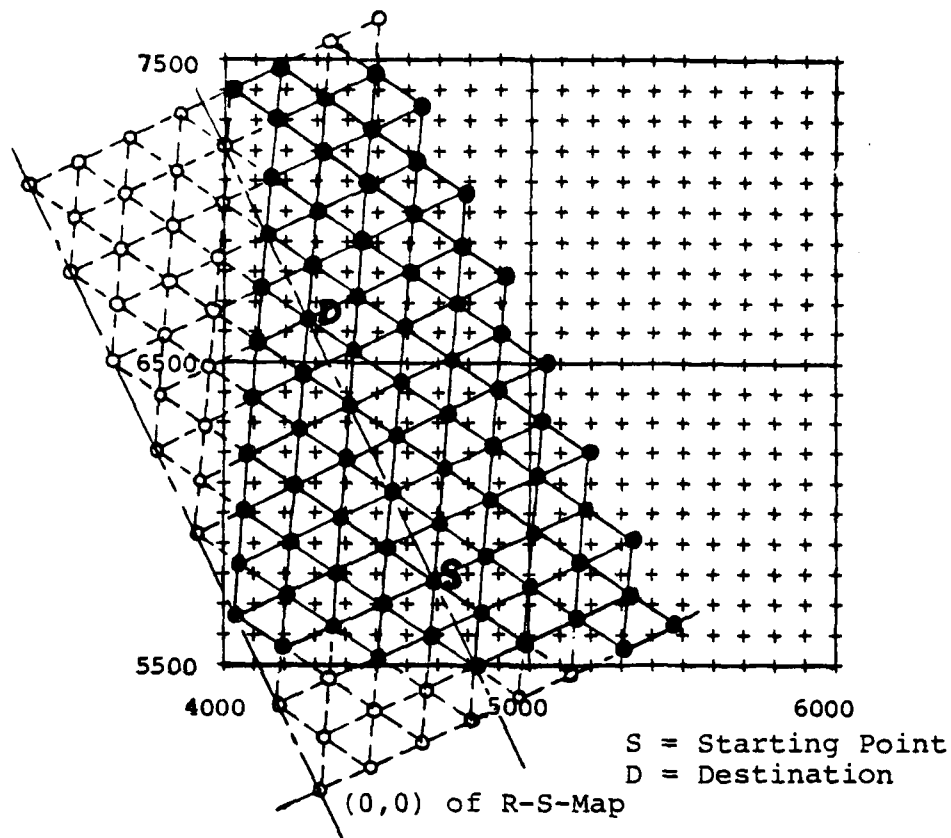
TR stands for Translated and Rotated into;

TP stands for Topographic map coordinates.

Explanations of these routines will be given in later sections to come.

C. OUTLYING NODES

As shown in Fig. IV-5, not all the nodes that have been generated fall within the boundaries of the topographic map. On other occasions, the combat simulation may have defined



NOTE: - Nodes with circle are outliers. They will be discarded later by the routine.
- Nodes with dots will be considered by the Dijkstra stage.

Fig. IV-5. Network Grid on Route Selection Map Overlaid on Topographic Map.

sectors on the battlefield, one for each maneuvering unit. Therefore, it is necessary to prevent those nodes from being considered in the route selection process.

Outliers are handled by means of transforming each node number into topographic coordinates and comparing those values with the boundaries of the battlefield (or sector). Thus, the outliers can be discarded by assigning values of zero in the NETGRD array, which records the internode relationship within the network representation (lines 138 through 151 in Appendix B). The zeroes will prevent the corresponding arcs from being enumerated in the selection process.

D. ROTATION AND TRANSLATION OF COORDINATE SYSTEM

Standard textbooks on Calculus or Linear Algebra give the formula for coordinate translation as:

$$X_{NEW} = X_{OLD} + X_{TRANS}$$

$$Y_{NEW} = Y_{OLD} + Y_{TRANS} \quad (F.IV-1)$$

where:

X, Y_{NEW} are the translated coordinates;

X, Y_{OLD} are the old/original coordinates;

X, Y_{TRANS} are the coordinates of the translated coordinate system's origin with respect to the old system.

For rotation of the coordinate system, the formula is in the form:

$$X_{ROT} = X_{ORIG} \times \cos ROT + Y_{ORIG} \times \sin ROT \quad (F.IV-2)$$

$$Y_{ROT} = -X_{ORIG} \times \sin ROT + Y_{ORIG} \times \cos ROT$$

or in the form (for the inverse of rotation):

$$X_{\text{ORIG}} = X_{\text{ROT}} \times \cos \theta - Y_{\text{ROT}} \times \sin \theta$$

$$Y_{\text{ORIG}} = X_{\text{ROT}} \times \sin \theta + Y_{\text{ROT}} \times \cos \theta \quad (\text{F.IV-3})$$

where

X, Y_{ROT} are the coordinates in the rotated state;

X, Y_{ORIG} are the coordinates in the original system;

$\cos \theta$ and $\sin \theta$ are the cosine and sine of the angle of rotation respectively.

Those formulas are then combined to obtain a set of equations for simultaneously translating and rotating the coordinate systems that are being used in the routine:

a. From topographic map into route selection map

(subroutine TPTRRS):

$$X_{\text{RS}} = (X_{\text{TOP}} - X_{\text{TRANS}}) \cos \theta + (Y_{\text{TOP}} - Y_{\text{TRANS}}) \sin \theta$$

$$Y_{\text{RS}} = -(X_{\text{TOP}} - X_{\text{TRANS}}) \sin \theta + (Y_{\text{TOP}} - Y_{\text{TRANS}}) \cos \theta$$

(F.IV-4)

b. From R-S-map into topographic map (subroutine

RSTRTP):

$$X_{\text{TOP}} = X_{\text{RS}} \cos \theta - Y_{\text{RS}} \sin \theta + X_{\text{TRANS}}$$

$$Y_{\text{TOP}} = X_{\text{RS}} \sin \theta + Y_{\text{RS}} \cos \theta + Y_{\text{TRANS}}$$

(F.IV-5)

E. SUBROUTINE NNXFOG

Since the origin of the R-S-map has been defined to be coincident with node #1, the transformation of node number into the orthogonal R-S-map coordinates is straightforward and requires no further elaboration.

F. SUBROUTINE OGXFNN

This subroutine was initially devised in case the need arose to transform orthogonal coordinates into node number. In the present status, the route selection routine does not need this subroutine.

However, it is anticipated that whenever a formation control routine is developed, this routine will be required at that time.

G. SUBROUTINE SEGOPT

1. Segment Representation

Each route segment is represented by three points along the segment, in the order of movement direction:

- a. Current point (NODNOW);
- b. Mid-point of the segment ("MID").
- c. Node at the other end of the segment (NODNXT);

One can also represent a segment by a single point, either by one of the ends or by the mid-point. The three point representation has the purpose of enhancing the accuracy of the route selection logic.

2. Recommended Rate of Advance

For a particular segment, rate of advance is taken to be the average of the three values obtained (one for each point of the three point representation). If any of those values is zero, it can be concluded that a part of the terrain with zero passability is being encountered; thus the cost value

should be set high (=99.9) and the optimum speed is set at zero, preventing the logic from routing through this region.

3. P(killed) due to Defending Unit

Logically, a maneuvering unit should have expected enemy concentration in the vicinity of the destination point. In the real world the unit will not hesitate to move into this region.

Thus, the fact that there exists enemy concentration should not interfere with the route selection process. In other words, the maneuvering unit may seek fields of fire with the enemy during the final assault. The routines "mimic" this by not considering P(killed) due to those units (elements) that are located in the vicinity of the destination point. Thus, only those enemy outposts have influence upon the route being selected.¹⁴

"Vicinity" is defined as the region within the "assault-range" (ASSR) from the destination point. This variable is again user defined. In the exercise, a value of 500 meters is used.

¹⁴It was found in the experimentation with this routine that with the effects of the defending units (elements) in the vicinity of the destination point, results in the obtaining of a circling, spiral-like route. The phenomena is similar to that of a hiker climbing to a high peak in a circling manner to conserve strength. This is understandable since the trade-off performed by SEGOPT routine (for the hiker: trade off between distance traveled and climbing steepness) makes the route selection process sensitive to "elevation" (i.e., threat gradient) and would act in a similar manner to that of the mountain climber.

SEGOPT also tests whether the current segment is under influence of the defending unit being considered.¹⁵ Test of range is also done to make sure that the segment in question is not out of range of the defending unit. Aspect angle is also an influencing factor on the $P(\text{killed})$ due to enemy. It is widely known that a tank, due to its armor placement, is much more vulnerable to shots that come from directions of more than 30 degrees as compared with other directions. Hence, in the exercise, $P(\text{killed})$ due to enemy with aspect angle of more than 30 degrees is taken to be three times as large as that from other directions.

After the determination of the openness factor (see Chapter V.A.4), which is an average of three values, Equation F.III-1 is then applied and computed to obtain $P(\text{killed})$ due to enemy at a given rate of advance. This will be added to PKVEL, the probability of being killed by terrain at the same rate of advance to obtain total $P(\text{killed})$. The rest is a matter of sorting the various values of total $P(\text{killed})$, choosing the smallest one and transferring the corresponding Rate of Advance (i.e., Optimum rate of advance) to the (calling) Dijkstra routine.

¹⁵The criterion is whether or not the segment in question is in the "shadow" of a large object (hill, dense wood) that makes the defending unit unable to detect or to shoot at a maneuvering element in the segment.

V. MODEL EXERCISE

A. INPUT DATA

It was initially intended that this model be exercised as part of a large combat model, the STAR Model, being developed by the U.S. Army at the Naval Postgraduate School. However, nonavailability of the Naval Postgraduate School computer due to equipment upgrade made that impossible. As a result, it was decided to exercise the model in a "stand alone" version using "typical" terrain created for this purpose.

The terrain created consists of:

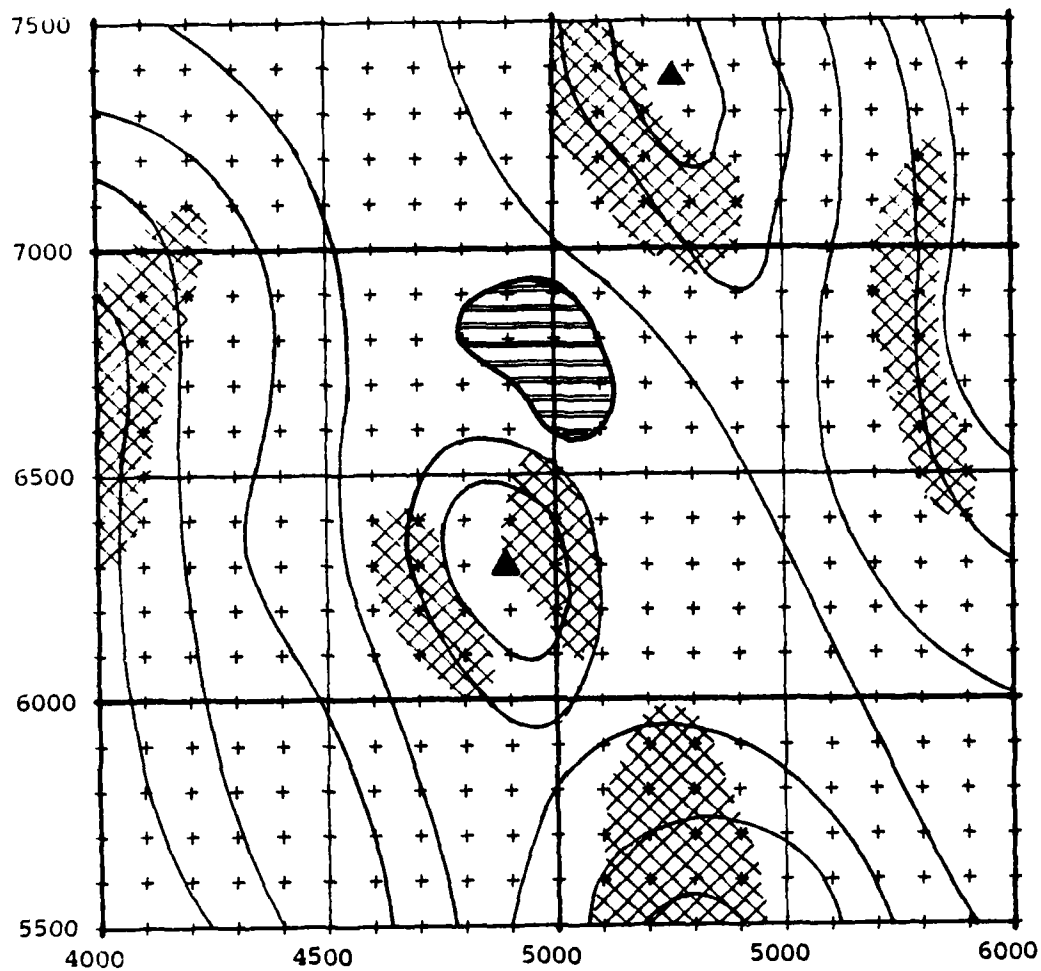
1. A Topographic Map of the Terrain

The map used was prepared only roughly and consists of hilly terrain with valleys, wooded areas, and a lake. It is illustrated in Fig. V-1.

2. A Map of Recommended Rate of Advance (MAPRSP)

This consists of a discrete mapping of the recommended rates of advance plotted on 100 meter grids on the topographical map. The entire map area includes a 2000 meter x 2000 meter area represented by 400, 100x100 meter grids.

Areas of low and high passabilities are plotted with respect to the location of woods, lakes, valleys and hills. Influences due to (imaginary) areas of low bearing strength soil (resulting in low passability) are also included.



LEGEND:

▲ hilltop

▣ woods

— lake

Fig. V-1. Topographic Map Used in the Exercise.

The resulting MAPRSP values are displayed in Appendix C. A characterization of the map is illustrated in Fig. V-2.

3. Map of Defending Unit's Influence (MAPINF)¹⁶

The influences exerted by (at most) two units of the defending force will be considered. Each unit considered has a map associated with it which represents the portion of terrain over which the unit has influence. The map consists of values of "1" (indicating that the unit has influence on the corresponding grid) or "0" (the unit has no influence). These values are determined considering masking offered by hilltops, dense woods, etc. A grid masked from the defending unit's location by a hill or by a densely wooded area is considered to be uninfluenced by that unit, and is given a value of "0," etc. A vehicle traversing a grid assigned a value of "0" is considered to be undetectable by the defending unit (thus invulnerable to that particular defending unit's weapon).

Since multiple defending units can be considered in this model (or multiple elements if the modeling is done at that resolution) the variable which contains the influence map, MAPINF, is three dimensional. The first dimension

¹⁶The influence factor is analogous to whether LOS exists from the observer to the points along the route segment under consideration.

4	2	7	10	11	11
6	5	9	12	12	11
7	9	12	15	15	13
0	7	11	14	12	13
0	8	12	15	14	13
0	9	12	14	12	10

Fig. V-2. Map of Recommended Rate of Advance (MAPRSP).

1	1	0	1	1	1
1	1	1	1	1	1
1	1	1	1	1	1
1	1	1	1	1	1
1	1	1	1	1	1
1	1	1	1	1	1

Fig. V-3. Map of Influence of One defending Unit (MAPINF).

1	1	1	2	7	8
1	2	2	6	9	8
3	3	4	7	8	7
5	7	6	8	9	7
8	9	9	8	7	6
9	8	9	9	8	7

Fig. V-4. Map of Openness of the Terrain (MAPCON).

represents the unit or element number,¹⁷ the last two dimensions represent grid coordinates.

4. Map of Openness of the Terrain (MAPCON)

Moving on a desert, a vehicle can be observed almost all the time regardless of the observer's position. Hence, a particular route segment may have 100% openness. In case of a digitized terrain, a grid may also have 100% openness. In other words, a vehicle moving anywhere in that grid will be exposed 100% of the time.

The situation will be different for a grid of other terrains, such as that used in the STAR Model. Due to the existence of vegetation and minor terrain variation, a vehicle traveling on a certain grid will be exposed to any observer only for a fraction of the total time needed to traverse through that grid. Hence, an openness factor which represents this phenomena could be obtained by measuring these fractional values a great number of times for various observer's locations and various directions of travel, and taking the average value afterward.

¹⁷In this simple exercise, it is considered sufficient to work with defending units instead of elements. If one wishes, the routine can be simply changed to allow consideration of defending elements. This is done by:

a. Providing each defending element with its own map of influence, or, in the case of STAR Model shooting a number of LOS's from each defending element to every segment of interest.

b. Setting the values of NDEFDK(I) at 1 for every element (I).

c. Changing the dimensionality of MAPINF to conform with the number of defending elements.

Corresponding to the concept of "terrain openness" is a parameter "probability of complete trace concealment," introduced by the Defense Mapping Agency. This agency has measured these values for most European terrain. For modeling purposes, the terrain openness factor can be regarded as equal to $(1 - \text{probability of complete trace concealment})$; hence, a modeler who has access to the data can readily develop a map of terrain openness.

5. Other Significant Input Data

These are listed below:

- PKVL is the probability of being killed by terrain (or more precisely: "not by enemy") at normal operating speed, i.e., at less than or equal to the value recommended by MAPRSP;
- RANGEM, the maximum effective range of the defending weapon system. A value of 4000 meters is used in this exercise.
- ASSR, the assault range; within this radius around the destination point, the "close-in" phase of the combat is considered to take place. Located within this region, a defending unit is considered to have no influence on the route being selected.
- FCYCLE, the firing cycle of the defending unit, input as time between rounds fired by the defending weapon system. Taken to be 20 seconds in this exercise;
- PKFOE, see Chapter II.E for explanation.

B. MODEL EXERCISE AND RESULTS

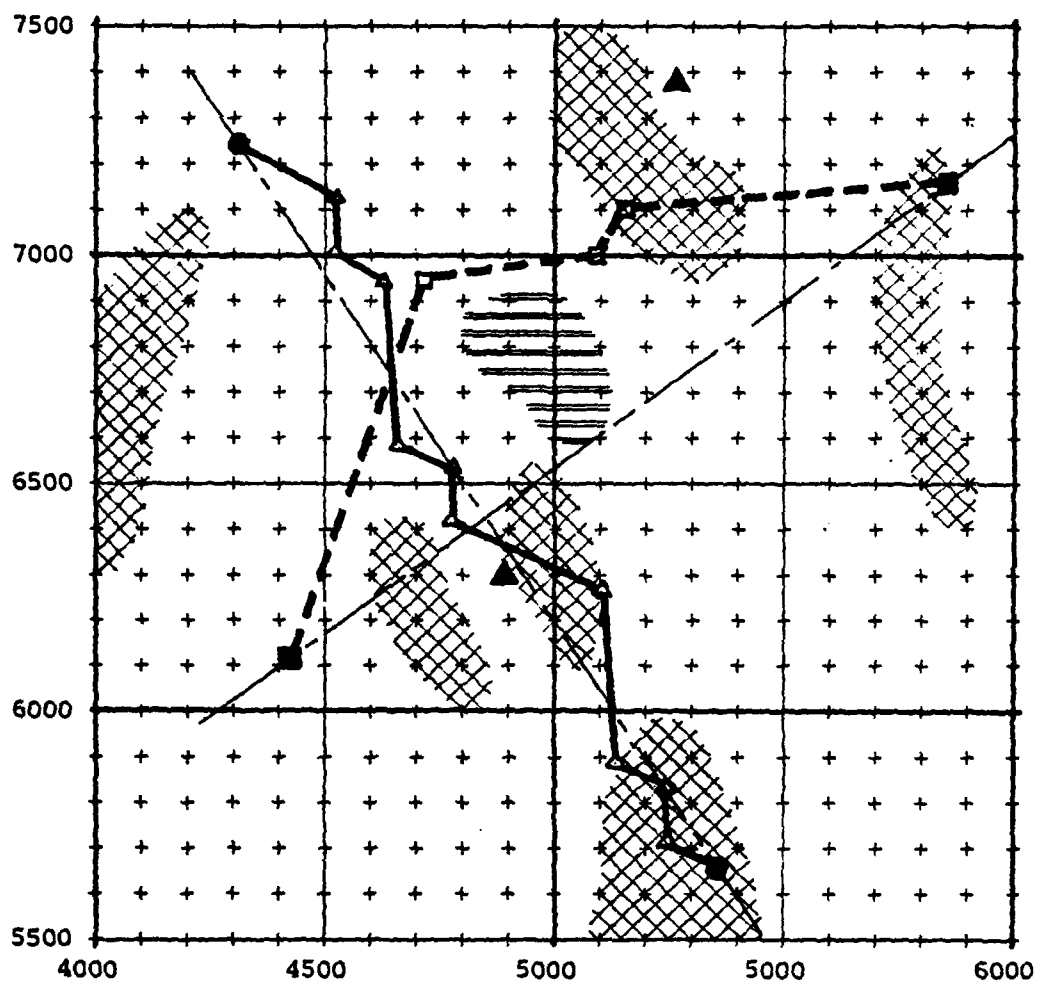
The developed model was exercised in a "stand alone" mode to demonstrate a number of aspects of route selection:

- Coordinate manipulations and reversibility;
- Variations of segment size;
- Variations in strength of one "threat-source" (defending unit);
- Variations in strength of two "threat-sources."

1. Exercise 1. Coordinate Manipulation and Reversibility

When attached to a combat simulation such as the STAR Model, it is anticipated that some problems of compatibility in coordinate manipulations and direction of travel would be experienced. Hence, it is important to test this newly developed routine under the full range of conditions that might be experienced in the combat simulation, particularly those conditions which might generate computational overflow or underflow in the model due to direction changes. Results of these tests are described below:

Appendix D-1 gives results of the first trial. The starting point is given to be (4310.0; 7237.0) and the destination is at (5355.0; 5670.0). The general movement direction is about Northwest-Southeast. As shown in the Appendix the routine successfully delivered the selected route in terms of both topographic map coordination and node numbers. The selected route (S1-D1) is also illustrated in Fig. V-5.



Note : to maintain clarity, only those corner-points of each route are plotted.

Fig. V-5. Exercise #1 : Coordinate Manipulations and Reversibility.

Appendix D-3 has a different set of starting and destination points which are (5870.0; 7170.0) and (4320.0; 6109.0). The direction of movement is about Northeast-Southwest. Again, the routine successfully delivered the selected route in terms of topographic-map coordinates and node numbers (see Fig. V-5).

Appendix D-4 is the result of testing the routine's capability in coordinate manipulation with a very small angle of rotation of the coordinate system. With the starting point at (5870.0; 7161.95) and the destination at (4320.0; 7161.92) the angle of rotation is only about $(0.03/1550.)$, or 0.0000193 radians. As presented in Appendix D-4 the routine successfully handles these conditions.

The conditions represented in the tests above are typical of those which would tend to cause compatibility errors between this routine and a combat simulation. Particular interest was given in reducing the change of underflow/overflow type errors by minimizing the utilization of trigonometric functions in the routine. As part of that effort, where directional information is required, the Pythagorean formula is used. Additionally, the majority of the movement calculations in the routine involve only the node numbers of the network grid.

Appendix D-2 contains the result of testing the routine for reversibility of routes. The result of reversing the starting point with the destination point is compared

with the "D-1" trial. Comparison of the topographical coordinates of the selected routes illustrates that the two routes are in fact the reverse of each other.

2. Exercise 2. Variations of Segment Size

Segment size, i.e., the length of each arc in the network grid, is a user's input to this routine. As previously discussed, the smaller this value becomes, the closer the resulting route is to globally optimum.¹⁸

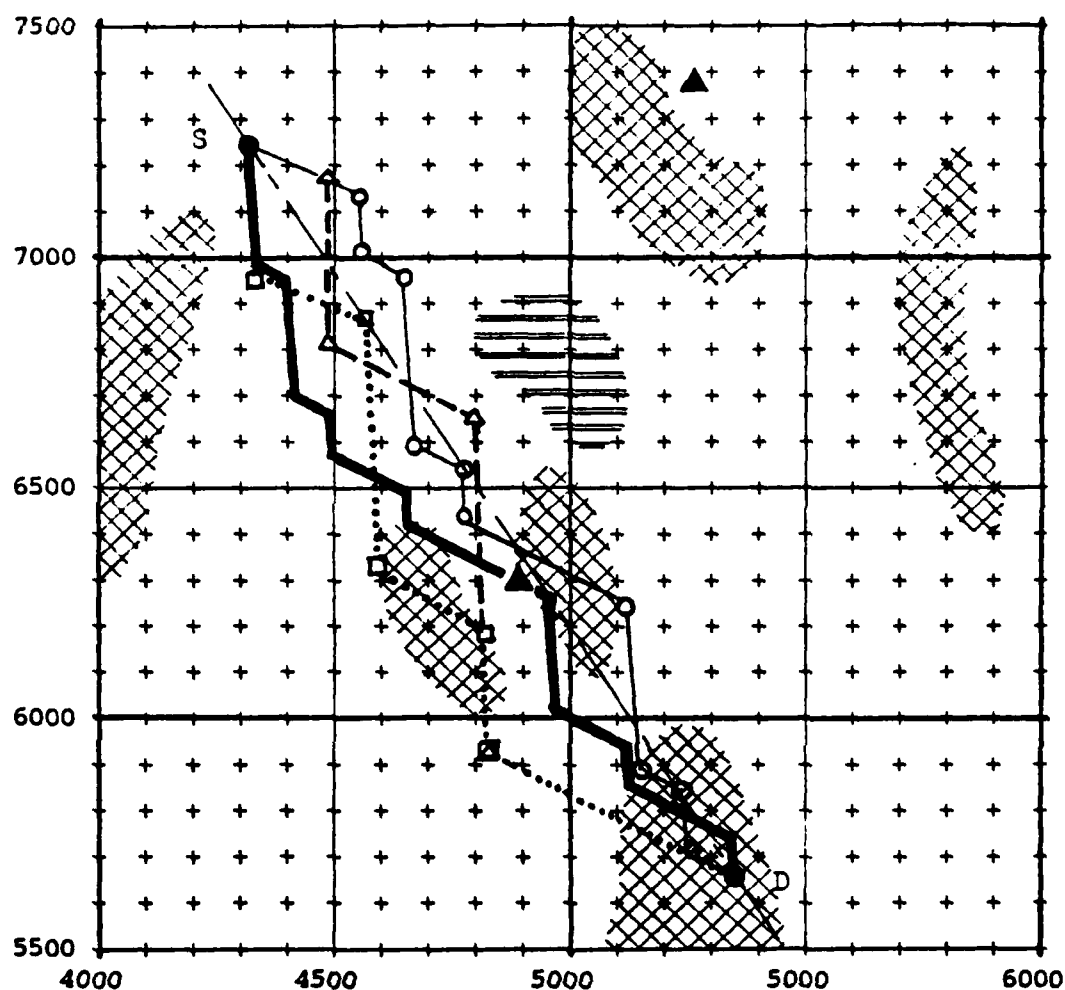
Appendix D-5, 6, 7, and 8 give the result for a fixed set of conditions with only the segment size varied (240, 160, 120 and 80 meters). The resulting routes are plotted and displayed in Fig. V-6. Those results illustrate that the shorter the input segment, the closer the resulting route to the best route so far obtained, i.e., the thick solid line (for SEGSIZ = 80m).

In this exercise there is little point in reducing the segment size (SEGSIZ) beyond 80m, since the grid size is set at 100 meters.

3. Exercise 3. Varying the Strength of One Defending Unit

Appendix D-9 through 12 gives the results of varying the strength of one enemy unit known to the advancing unit. The routes obtained are plotted in Fig. V-7. The solid line shows a route for the case of no knowledge of any defending

¹⁸In this routine SEGSIZ and Distance (from Start to Destination) determine the size of the Network, i.e., the number of nodes possessed by the network.



LEGEND :

- ==** Lake (zero passability)
- for segment size = 240m.
- △** for segment size = 160m.
- for segment size = 120m.
- for segment size = 80m.

NOTE : To maintain clarity, only those corner-points of each route are plotted.

Fig. V-6. Exercise #2 : Varying Segment Size (Input).

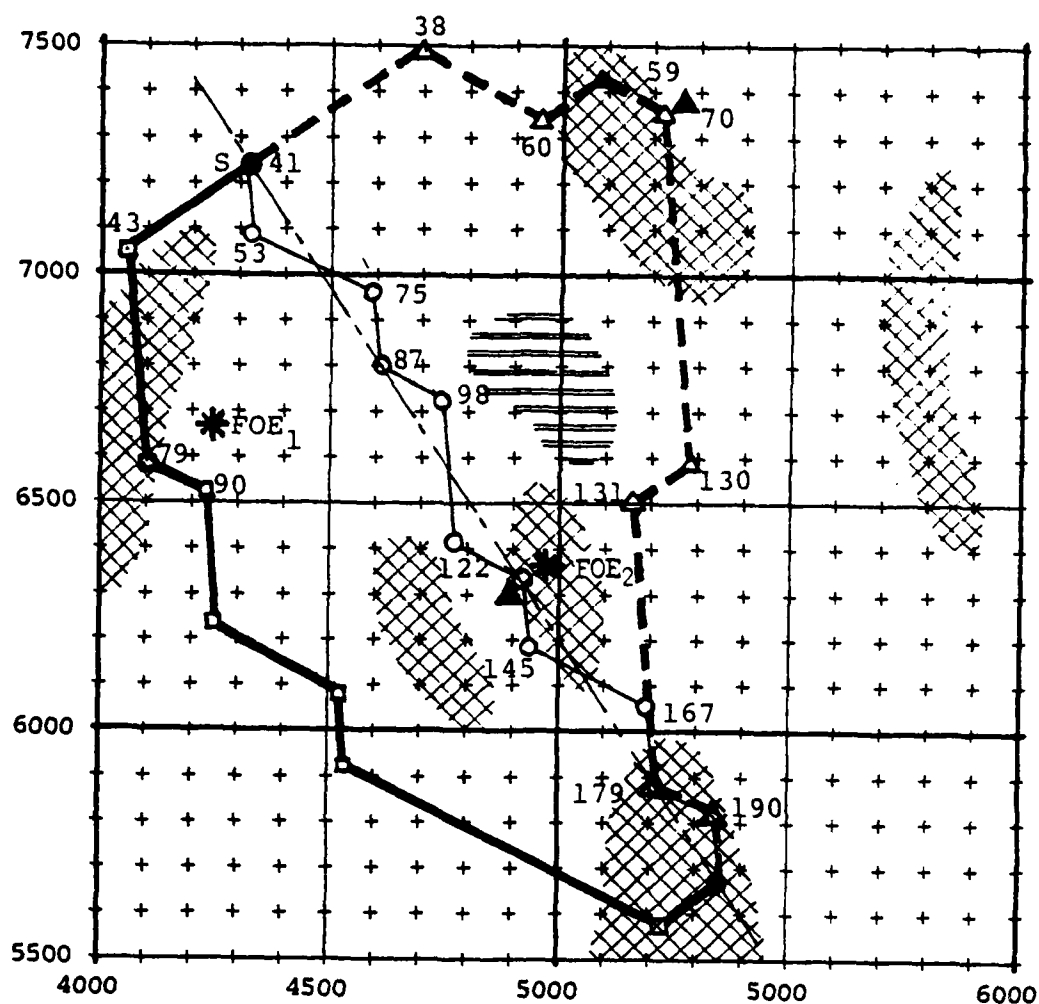
unit, but it is also the route obtained with knowledge of up to three enemy elements located at FOE1.

One may have anticipated that the route would begin to "bulge" outward at the knowledge of even a single enemy element. However, this does not occur due to the existing lake in that region (shown by the doubly shaded area). Going around the northern and eastern side of the lake may be more costly when compared to the solid line route, even with the knowledge of three enemy elements (the advancing unit has 36 elements in this exercise). The unit "stays" in the main route, until it is given the knowledge that four enemy elements are present at FOE1. With four enemy elements at FOE 1, it becomes less costly to go around the lake (extending the traveling distance). Additionally, the new route passes through node 60-59-70 where dense wood exists, protecting the maneuvering unit from FOE1's threat.

The route stays the same for greater threats since the number of alternatives is limited due to space restrictions imposed by the triviality of the map.

4. Exercise 4. Varying the Strengths of Two Defending Units

Figure V-8 shows various routes that are selected, based upon the knowledge of each threat source. The route selected when no knowledge of threat is given is (41-53-75-87-etc.). Knowledge of a single threat source was discussed in the preceding section.



- - Knowing no defending unit.
- - Knowing one or more elements in FOE₂, none in FOE₁.
- △ - Knowing four or more elements in FOE₁, none in FOE₂.

FURTHER: For $(FOE_1/FOE_2) > 4.5$ route □ will be taken

< 4.5 route △ will hold

NOTE: 4.5 is only rough estimate for this particular situation (see discussion).

Fig. V-8. Exercise #4. Variations in Two Defd. Units' Strength.

Knowledge of the single threat at FOE2 results in the route (41-43-79-etc.), which is clearly a better one than route (41-53-75). From node 90 through node 202 the advancing unit is protected by the hill just behind FOE2. Note that this route passes in close proximity to FOE1, the advancing unit has no knowledge of the threat at that location.

An interesting result is observed when both threat sources are known to be present. When FOE1 and FOE2 have strength ratio of 1:1, the route selected is the right hand one (41-43-79-etc.). When the strength of FOE1 is increased four fold (strength ratio of 4:1), the selected route remains the same. The logic appears to select a path directly onto one threat source when it is apparent that:

- the second threat source (FOE2) will soon be inactivated, i.e., when the advancing unit reaches node 90;
- it is less dangerous to face one threat source directly (with the other threat coming from the flank) rather than be subjected to two threats simultaneously coming from the flank, as would be the case with route 40-38-etc.¹⁹

¹⁹ Note that P(killed) with aspect angle of larger than 30 degrees is taken to be three times as large as otherwise, due to armoring in the front of the vehicles.

Sensitivity analysis in this situation demonstrated that the route remains constant until the ratio of the defending elements at FOE1 to that at FOE2 is 4.5:1. With a strength ratio of 5:1 the selected route becomes 41-38-60-etc. It should be noted here that the triviality of the prepared terrain has given rise to a limited number of alternatives in the route selection process.

Reasonable results in the "stand alone" exercises of the model, which are discussed above, indicate that this routine could be successfully implemented in a combat simulation. Hereafter, the problem is one of "hooking" it up to the selected combat simulation. That problem will be discussed in the next chapter.

VI. USE OF THE MODEL

The implementation of this route selection model in an existing combat simulation may require adjustments to both this routine and the receiving simulation in order to insure compatibility. The task of insuring that the combat simulation provides the proper environment for the route selection routine will be discussed in the following section. Potential modifications to the route selection routine are discussed in Chapter VI.B.

In order to make movement of elements more realistic, a routine to control the tactical formation of the advancing unit may be required. A discussion of a potential concept for the development of such routine is presented in Chapter VI.C.

A. PREREQUISITES FOR USE OF THE MODEL

In order for the route selection routine to work properly, it must be provided with certain input as described below:

1. PKFOE Data

The threat data representing probability of being killed by enemy elements is absolutely necessary for the route selection routine. As previously discussed, PKFOE is one of the two trade-off parameters (PKVEL, probability of being killed due to terrain or overspeeding is the other)

utilized in developing the selected route. A description of the variable was presented in Chapter II.E. In the route selection process, the degree of optimality of the selected route depends partly on the accuracy of the estimate of PKFOE.

If a rough estimation of PKFOE is considered sufficient, the outline presented in Chapter II.E may be used to generate PKFOE. If a high degree of accuracy is desired, a more thorough analysis may be needed to determine PKFOE from a number of the parameters involved. Some of those parameters are:

- distance to threat location;
- speed being executed;
- direction of travel and aspect angle;
- weapon system specifications;
- terrain-vegetation;
- weather conditions;
- contrastness of vehicle to its surrounding.

Developing more accurate estimates for PKFOE, considering all the parameters above, is beyond the scope of this thesis and would require an additional level of effort equivalent to this one.

2. Recommended Rate of Advance Data

In a combat model like "STAR," limiting speed associated with each pair of coordinates is presently computed as part of the model's movement algorithm. That parameter

can be considered as a reflection of the recommended speed at a particular location.

If "SPEED-LIMIT" (at a given location) is defined as the speed at which the ultimate capabilities of driver and vehicle are being exploited, then there exists a speed at which the driver and vehicle could perform satisfactorily without excessive strain and without endangering their vehicle. This speed is what is meant by "recommended speed" in the route selection model.

If a rough estimate is permissible in a particular Combat Model like "STAR," a fraction of the "SPEED-LIMIT" may be regarded as the "recommended rate of advance." The "SPEED LIMIT" itself corresponds to the preset value "27" used in the SECOPT subroutine representing the maximum rate of advance at any given location. This arrangement prevents the route selection model from delivering an optimum speed larger than "SPEED-LIMIT."

Hence with very slight modification, by calling the "SPEED LIMIT" subroutine in the STAR Model, the route selection routine may obtain the value of the recommended rate of advance needed for a segment under consideration.

3. Maps of Influence and Openness of Terrain

On a continuous terrain like the one used in the STAR Model, the influence and openness parameters can be combined into a single value. Recall that these parameters are used in the determination of PKVOE. The combination of these two

factors provides a measure of how well a defending unit controls the route segment under consideration.

On a continuous terrain an equivalent result can be obtained by computing a number of lines of sight (LOS's) from the particular defending element to equidistant points along the segment under consideration (e.g., 7 LOS's). An overall exposure factor can then be determined by averaging the percent exposure obtained for each of the seven LOS's. The aggregate value (also in percent) is a measure of how well the segment is being controlled by the defending unit. In the route selection routine, this is equivalent to:

$(\text{linf} \times \text{Openness Factor})$

4. Attrition Due to Terrain

Since this route selection routine is based upon the trade-off between attrition due to enemy and attrition due to terrain, it appears logical to require that the combat simulation also considers both factors.

While most combat models consider the first factor, very few consider vehicle attrition due to terrain.

Using information currently available in the route selection routine that capability is not difficult to implement. By drawing random numbers, one for each vehicle for each mile covered along a segment, and comparing it to $P(\text{killed}) = PKVEL$ computed in the SEGOPT subroutine, the required attrition values can be developed. This procedure is acceptable for implementing this effect in an event step

simulation. Implementation in a time step simulation would be similar, with little additional effort.

B. MODEL ENRICHMENT AND EXPANSION

The author believes that the version of the route selection model presented herein represents a good initial iteration of the particular approach utilized. Modification or expansion would be required, however, to increase resolution and capability. A number of possible improvements are discussed below.

1. Degree of Resolution

A single variable NTEMP (line 72-74 in the listing, Appendix B) determines the degree of resolution of the route selection model. As can be seen from the logic, NTEMP is determined by two variables, distance from starting to destination point and SEGSIZ (see Nomenclature in Fig. IV-4).

Further, since the network generated has been standardized in shape, NTEMP and the size of the network have one-to-one relationship. NTEMP is currently limited to a value of 17, which is related to the maximum of 925 nodes in the network grid.

For higher resolution, it is necessary to change both the limitations on NTEMP (line 72-74) and some of the array dimensions in the routine. The array dimensions involved are those of NETGRD, TOPOG, LABLFF, LABLFP, FCOST, OFTSPD, XROUTE and OPRADV variables. The changes should be done in accordance to the following formula:

$$\text{Max \# of nodes} = 2 \times (\text{NTEMP} + 4.5)^2 + 1 \quad (\text{F.VI-1})$$

For example, if NTEMP were changed to 34, the number of nodes in the network grid would be 2965. Hence, doubling the limiting value of NTEMP results in array dimensions that are more than tripled. This example illustrates that memory usage of the computer changes progressively with the limiting value of NTEMP. Users should be aware of this impact.

2. Consideration of Path Gradient

If desired, this routine can be modified to take gradient changes in a route into consideration in the selection. A slope-factor, which is included in formula (F.III-1) is required for this. Further, in order to restrain the routine from choosing too steep a path, the implementation requires consideration of the following:

a. Whenever a segment has a gradient larger than the maximum specification of the vehicle, traveling cost within that segment should be set at 99.99 and the optimum speed to 0.0. This is done in SEGOPT subroutine.

b. For other situations, the penalizing factor (slope-factor) will apply within the formula (F.III-1), which is also in the SEGOPT-subroutine. The penalizing effect should be smaller on a descending segment than on an ascending one.

3. Playing With Defending Elements

In the presented results the routine was exercised with defending units rather than with defending elements. At present the number of the defending unit is limited to six (see the Dimensions of NDEFDK, XDEFDK, YDEFDK in the listing).

It is anticipated that some users might want to play at a higher level of resolution, to consider defending elements. To do this the user need only change the dimensions of MAPINF (if it is still being used; see Chapter VI.A.3), XDEFDK, YDEFDK and NDEFDK to conform with the number of defending elements included. Further, each value of NDEFDK should be set = 1 (integer).

The user should again be aware of the progressively increasing demand for resources due to this expansion. In this case it is manifested in terms of increased run time.

4. Diversifying the Defending Weapons

In the real world the defending force employs numerous weapon systems with various effectiveness and ranges. The advancing unit's elements are, therefore, subject to differing threats imposed by each of the weapon systems. In order to enable this routine to handle such a situation, it would be beneficial if the user could assume additivity of threats (from the various weapon types) on the moving elements.

This situation could then be handled with the following modification:

- a. For each defending location (element) an additional attribute "WEAPON-TYPE" must be assigned;
- b. For each weapon type deployed, one PKFOE-table must be prepared;

c. For each weapon type a RANGEM-value (max weapon's range in meters) must be assigned; thus, RANGEM becomes an array with dimension equal to the number of types of weapons.

With slight modification in computations (SEGOPT subroutine) this route selection routine should easily be able to handle this situation.

5. Diversifying the Maneuvering Elements

Again, in the real world, a maneuvering unit should consist of various types of elements. Furthermore, each type of element could be expected to have different characteristics in terms of speed, size and armor type. Consideration of more than one type of element would greatly enhance the resolution of the model.

The author believes that this would be the limit of the expandability of this route selection routine. An expansion of the logic structure is needed before this additional capability can be handled satisfactorily (after the task discussed in the following section has been accomplished).

This limitation is imposed by the fact that the present routine treats the maneuvering unit as a single element (point wise route selection). Hence, the size and structure of the route selection algorithm utilized in the model would require modifications. These modifications would have to be made in the context of formation control as discussed in the next section.

C. THE PROBLEM OF FORMATION CONTROL

Although the task of actually implementing formation control is beyond the scope of this thesis, the problem (in conjunction with the route selection) is discussed at the conceptual level below. The actual development of a routine to handle formation control in a combat simulation model would make an interesting topic for future thesis effort.

In discussing the formation used by a maneuvering unit, one should logically consider each element in that unit. Element-wise handling by calling the route selection routine for each element may lead to a set of "optimal" routes, one for each element. However, this set of "all optimal" routes could lead to separation of the maneuvering elements, thus violating the formation dictated by the unit commander (or higher echelon commander).

On the other hand, strictly maintaining the formation (thus an additional constraint for every call of the route selection routine) may induce the selection of a set of routes which may be far from "all optimal." Some of the routes might even be infeasible.

At this point, two approaches in handling this problem are apparent:

1. The first approach is to determine a set of routes, one for each element, without violating formation of the unit (hence, formation becomes an additional constraint to

to the "compounded route selection" problem). In this situation it may turn out that no set of "all-optimal" routes satisfy the constraint. Thus, the model has to face a trade-off scheme:

a. Loosen the formation constraint, yet maintain the "feasibility" of each route (optimality is no more an issue here);

b. Strictly comply with the formation constraint, but accept less than "satisfactory" routes.²⁰

In order to allow the user to employ a technique consistent with his own preference, the best approach here would be to allow the model to work in either mode, based on user input.

An algorithm for option a is presented in Fig. VI-1, one for option b is presented in Fig. VI-2.

2. A second possible approach is to handle the route selection and formation control simultaneously. In this concept, the unit is considered as a big mass (instead of a single point), moving through the combat-terrain. The scheme would be similar to that used by the route selection routine presented in this thesis.

²⁰If this line of thought is chosen, then the modeler must define the satisfactory level for a route for each type of element such that the routine fulfills the March-Simon Hypothesis (Ref. 1, pp. 5-21):

***most human decision making whether organizational or individual is concerned with the discovery and selection of "satisfactory-alternatives; only in exceptional cases it is concerned with the discovery and selection of "optimal alternatives."

ALGORITHM A

1. Choose one optimal route (pointwise selection).
2. At each node-member of this route probe the width of available passage¹ (to the left, to the right, then sum up).
3. CHECK: Does every node "provide" sufficient passage?
 - a. YES: Deliver the route, the rest will be taken care of by Formation Control; STOP.
 - b. NO : Record this route and its "passages;" GO TO 4.
4. CHECK: Has Level of Exhaustion of Search been reached yet?
 - a. NO : "Pull" out every infeasible node² from the Network Grid; GO TO 1.
 - b. YES: Select (from the records) one route having minimum level of violation³ of formation. Deliver; STOP.

¹A 'passage' is defined as the available width in the neighborhood of the current node which will be accessible to the advancing unit without exceeding a certain level of threat ($P(\text{killed}) - \text{total}$).

²"Infeasible-nodes" are nodes which offer insufficient width of passage.

³Minimum level of violation could be predefined in number of infeasible passages the route possesses and to what level of violation of formation.

Fig. VI-1. Algorithm A (see text)

Fig. VI-1. Algorithm-A (see text).

ALGORITHM B

1. Choose one optimal route (pointwise selection) for the leading element.
2. Choose "parallel" routes¹ to this one, one for each of the other elements, strictly maintaining formation.
3. CHECK: Is every route feasible?²
 - a. YES: Deliver the set of routes; STOP.
 - b. NO : Record this set of routes; GO TO 4.
4. CHECK: Has Level of Exhaustion³ of Search been reached?
 - a. NO : "Pull" out every infeasible arc from each route out of the Network Grid; GO TO 1.
 - b. YES: Select one set of route with minimum infeasibility⁴. Deliver; STOP.

¹Parallel routes is defined by the formation dictated by situation.

²Feasibility is determined by tolerable threat ($P(\text{killed})$).

³Level of Exhaustion of Search may be defined by limiting the number of sets of routes that have been selected.

⁴Minimum infeasibility is determined by number of elements experiencing infeasibility and level of infeasibility.

Fig. VI-2. Algorithm-B (see text).

This unit mass would be located by a single point (maybe the leading element, or the center of mass). The entire unit would be assumed to follow the route selected for that point. Cost calculation would be made on each element considered separately in terms of physical location (relative to the point representing the unit location) and exposure to the threat.

The total cost could be obtained by pooling the threat experienced by each element.

This approach requires that a number of issues be resolved:

- What is the method of pooling?
- Since there are a number of types of elements, should weights be assigned?
- How should one determine those weights?

With those issues resolved satisfactorily, then the Dijkstra Algorithm can be employed and the element wise route selection is simply resolved.

In this situation, however, the modeler is still haunted by the same challenge previously confronting him:

a. Should the big mass be regarded as a rigid body, thus the formation is maintained strictly along the route?

b. Or should it be regarded as a "putty-like" substance where the big mass could yield and thin itself whenever the terrain could not accommodate all its (formation-defined) "frontage?"

The author has the opinion that in order to model the real world's advancing unit's behavior properly, the modeler should combine both options a and b. It is apparent that (see discussion in Chapter II.B) in the real world the formation is occasionally violated by some elements for the sake of maintaining the "satisfactory level" in the route being traversed. On the other hand every effort is made to maintain the formation.

Although time did not allow implementation of the improvements/expansions discussed above, the conceptual framework presented in each case should simplify future addition of those improvements/expansions to the basic route-selection model.

VII. CONCLUSIONS

1. A basic route selection model has been built successfully as part of this thesis. It has the following features:

- a. The route selected is in the form of a one vehicle movement route;
- b. The routine can work with any pair of starting and destination points, and with any direction of travel. Hence, it can be used for sequential route selection as well as a one-time route selection;
- c. The model is flexible enough to work with digitized terrain in its present form, and with continuous terrain with only slight modification;
- d. The movement influencing factors (mentioned in Chapter II.B) are taken into consideration in selecting the route;
- e. The selected route reflects some uncertainty with respect to optimality, a desired quality in modeling (error prone) human decision making.

2. In its present configuration the model includes a number of limitations. They are:

- a. Only single element movements are handled, not clusters of vehicles as is desirable to portray an advancing unit;

b. No capability exists to handle diverse types of threat weapon systems and maneuvering vehicles.

3. A number of ways of improving/expanding the model have been presented, and should be considered for follow-on thesis efforts.

APPENDIX A: LIST OF VARIABLES
(in alphabetical order)

ANGLFC	- (Aspect) Angle Factor
ASSR	- Assault Range (in the exercise = 500m)
ASSRR	- square of ASSR
COSROT	- cosine value of the angle of rotation of the coordinate system
COSTMN	- temporary cost value (to compare costs with)
DISQR	- square of distance
FCOST(I)	- forward cost (to destination) from the i-th node through the predecessor node stated in LABLFP(I).
FCYCLE	- firing cycle of the defending weapon system, taken to be 20 seconds in the exercise
JADV	- integer value of the recommended rate of advance in a segment being optimized by SEGOPT-subroutine
JFORWD	- in Dijkstra Algorithm, the node just being permanently labeled, currently being enumerated
LABLFF(I)	- initially: flag-value ("1" or "0") of the I-th node. After the completion of all Dijkstra enumerations, it is used as an array stating the node numbers belong to the selected route

LABLFP(I) - for the I-th node, LABLFP(I) records the predecessor with minimum cost at current status
 MAPCON(J,K) - shown the value of the openness of the terrain at location/pixle (J,K)
 MAPINF(I,J,K) - has values of either "1" or "0" that shows the influence of the I-th defending unit upon location/pixle (J,K)
 MAPRSP(J,K) - shows the recommended rate of advance at location/pixle (J,K) for a given vehicle
 NCNR - see Nomenclature in Fig. IV-4
 NCl - ditto
 NCOLHX - ditto
 NDEFDK(I) - number of defending elements in I-th location or unit
 NELATK - number of elements in the attacking-unit
 NETGRD(I,J) - interrelation array, shows to which nodes the I-th node has relations with
 NODEST - destination node
 NODSTR - starting node
 NROWHX - see Nomenclature in Fig. IV-4
 NTEMP - ditto
 CFTSPD(I) - optimum rate of advance from I-th node to its predecessor
 OPRADV(I) - optimum rate of advance in the I-th segment of the selected route.

PIXLE	- size of each pixle (100m sqrd)
PKFOE(I,J)	- P(killed) due to enemy as a function of speed (I) and distance (J)
PKVEL	- P(killed) due to "non-enemy" causes, i.e., terrain and overspeeding
PKVOE	- P(killed) due to enemy at a given rate of advance (in SEGOPT), not an array
PKVL	- P(killed) due to terrain (and overspeeding) for each mile of distance traversed (= .0002 in the exercise)
PKTOT	- total P(killed) (due to enemy and terrain/overspeeding)
RANGEM	- maximum range of the defending weapon system
RRANGE	- sequare of RANGEM
RADVN	- rate of advance
SDISTD	- distance between S (starting point) and D (destination)
SEGMEN	- input segment size (in meters)
SEGRT3	- SEGMEN x SQRT3
SEGSIZ	- modified SEGMEN, working segment size
SINROT	- value of sine of the angle of rotation
SUVCOS	- survival cost of the maneuvering unit (in terms of P(killed))
SQRT3	- square-root of 3.0
TOPOG(I,J)	- topographical (map) coordinate for I-th node of the network grid; J=1 for x-direction and J=2 for y-direction

TCOST	- temporary cost (for comparison)
XDEST	- (topographical) abscissa of the destination
XDEFDK(I)	- I-th defending unit's abscissa (x-direction)
XEAST	- most Eastern latitude in the battlefield
XORT	- orthogonal abscissa in the R-S-map
XRSJ	- location of origin (in R-S-map) w.r.t. the starting point in x-direction
XSTART	- abscissa (Topographic-Map) of the starting point
XWEST	- most Western latitude of the battlefield
YDEST	- (topographical) ordinate of the destination
YDEFDK(I)	- I-th defending unit's ordinate (y-direction)
YNORTH	- most Northern longitude in the battlefield
YORT	- orthogonal ordinate in the R-S-map
YRSO	- location of origin (in R-S-map) w.r.t. the starting point in y-direction
YSOUTH	- most Southern longitude of the battlefield
YSTART	- ordinate (Topographic Map) of the starting point

APPENDIX - B.

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NAVAL POSTGRADUATE SCHOOL MONTEREY CA

F/G 9/2

DYNAMIC ROUTE SELECTION FOR LAND COMBAT SIMULATION MODEL.(U)

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C...READING THE RECOMMENDED-SPEED DATA...
DO 140 I=1,20
  READ (5,115) (MAPRSP(I,J),J=1,20)
  115 FORMAT (20I2)
  140 CONTINUE
C...READING THE DATA OF THE DEFENDING-UNIT'S INFLUENCE...
DO 180 I=1,NLOC
  DO 160 J=1,20
    READ (5,116) (MAPINF(I,J,K),K=1,20)
  160 CONTINUE
  180 CONTINUE
C...DATA OF PKILL DUE DEFENDING-UNITS...
DO 220 I=1,28
  READ (5,121) (PKFOE(I,J),J=1,40)
  210 FORMAT (10F8.5)
  220 CONTINUE
C 6589 WRITE (14,6590)
C
C...DEFINING SOME CONSTANTS THAT WILL BE USED FREQUENTLY...
ASSRR = ASSR**2
SQRT3 = SQRT(3.)
SEGRT3 = SEGMENT*SQRT3
DISQR = (YDEST-YSTART)**2 + (XDEST-XSTART)**2
SDISTD = SQRT(DISQR)
SINROT = (XSTART - XDEST)/SDISTD
COSROT = (YDEST - YSTART)/SDISTD
RRANGE = RANGEM**2
C...DETERMINATION OF THE SIZE OF THE NETWORK FOR ROUTE-OPTIMIZATION...
NTEMP = (SDISTD/SEGRT3)
C...TO LIMIT THE SIZE OF THE NETWORK (MAX 925-NODES)...
IF (NTEMP.GT.17) NTEMP=17
  SEGRT3 = SDISTD/NTEMP
  SEGSI2 = SEGRT3/SQRT3
  IXESS = NTEMP - 2*(NTEMP/2)
  NCOLHX = NTEMP + 5
  NROWHX = 2*NCOLHX - 1
  NCI = NCOLHX - 1
  NCNR = NCOLHX*NROWHX - (NROWHX/2)
  NCCL = NCOLHX + NCI
  SEGCLC = SEGSI2/PCYCLE
C...W.R.T. X-,Y-START, THE ROUTE-SELECTION MAP HAS ITS ORIGIN AT :
  XORIG = -NCI*SEGSI2/2
  YORIG = -(4 - IXESS)*SEGRT3/2

```

```

RUT00420
RUT00430
RUT00440
RUT00450
RUT00460
RUT00470
RUT00480
RUT00490
RUT00500
RUT00510
RUT00520
RUT00530
RUT00540
RUT00550
RUT00560
RUT00570
RUT00580
RUT00590
RUT00600
RUT00610
RUT00620
RUT00630
RUT00640
RUT00650
RUT00660
RUT00670
RUT00680
RUT00690
RUT00700
RUT00710
RUT00720
RUT00730
RUT00740
RUT00750
RUT00760
RUT00770
RUT00780
RUT00790
RUT00800
RUT00810
RUT00820
RUT00830
RUT00840
RUT00850
RUT00860

```

```

C...DETERMINATION OF ORIGIN IN R-S-MAP W.R.T. THE ORIGIN OF TOPG.-MAP...RUT00870
CALL RSIRTP (XSTART,YSTART,SINROT,COSROT,XR50,YR50)
WRITE (14,6600) SDISTD,XR50,YR50
WRITE (14,6605) NTEMP,NCOLHX,NROWHX
RUT00880
RUT00890
RUT00900
RUT00910
RUT00920
RUT00930
RUT00940
RUT00950
RUT00960
RUT00970
RUT00980
RUT00990
RUT01000
RUT01010
RUT01020
RUT01030
RUT01040
RUT01050
RUT01060
RUT01070
RUT01080
RUT01090
RUT01100
RUT01110
RUT01120
RUT01130
RUT01140
RUT01150
RUT01160
RUT01170
RUT01180
RUT01190
RUT01200
RUT01210
RUT01220
RUT01230
RUT01240
RUT01250
RUT01260
RUT01270
RUT01280
RUT01290
RUT01300
RUT01310
RUT01320
RUT01330
RUT01340

C...DEFINING THE REFLECTING-ARRAY...
MIRROR(1) = 4
MIRROR(2) = 5
MIRROR(3) = 6
MIRROR(4) = 1
MIRROR(5) = 2
MIRROR(6) = 3

C...GENERATING THE NETWORK OF NODES AND ARCS (INTERNODE-CONNECTIONS)...
DO 300 K=1,NCNR
  NETGRD(K,1) = 1+K
  NETGRD(K,2) = K-NC1
  NETGRD(K,3) = K-NCOLHX
  NETGRD(K,4) = K-1
  NETGRD(K,5) = K+NC1
  NETGRD(K,6) = K+NCOLHX
  CONTINUE
300 DO 320 K=1,NCOLHX
  NETGRD(K,2) = 0
  NETGRD(K,3) = 0
  CONTINUE
320 NCNW = NCNR - NC1
  DO 340 K=NCNW,NCNR
    NETGRD(K,5) = 0
    NETGRD(K,6) = 0
    CONTINUE
340 NCC1 = NCOLHX + NC1
  NNC1 = 2*NC1
  DO 360 K=1,NCNW,NCC1
    NETGRD(K,3) = 0
    NETGRD(K,4) = 0
    NETGRD(K,5) = 0
    KTEMP = K + NC1
    NETGRD(KTEMP,6) = 0
    NETGRD(KTEMP,1) = 0
    NETGRD(KTEMP,2) = 0
    KTEMP = K + NCOLHX
    NETGRD(KTEMP,4) = 0
    NETGRD(KTEMP,5) = 0
    KTEMP = K + NNC1
    NETGRD(KTEMP,1) = 0
    CONTINUE
360
C...DETERMINATION OF STARTING NODE(-NUMBER) IN THE OPTIMZ.NETWORK.....
370 NOODSTR = (4.5-IXESS)*NCOLHX - 1

```

```

C...DETERMINING THE DESTINATION NODE(-NUMBER)...
C   NODEST = NODSTR + NTEMP * NCC1
C...NODES OUTSIDE THE TOPOGRAPHIC MAP SHOULD BE DISCARDED...
DO 460 I=1,NCNR
  CALL MNXFOG(SEGRT3,SEGSIZ,NCOLHX,NCC1,I,XI,YI)
  CALL RSTRIP (XRSO,YRSO,SINROT,COSROT,XI,YI,XIN,YIN)
  TOPOG(I,1) = XIN
  TOPOG(I,2) = YIN
  IF (XIN.LT.XWEST.OR.XIN.GT.XEAST) GO TO 420
  IF (YIN.GT.YSOUTH.AND.YIN.LT.YNORTH) GO TO 460
C...THIS POINT LIES OUT OF THE BATTLEFIELD...
430 DO 450 J=1,6
  NETGRD(NETGRD(I,J),MIRROR(J)) = 0
  NETGRD(I,J) = 0
450 CONTINUE
460 CONTINUE
C...START WITH THE DIJKSTRA-ALGORITHM...
C...INITIALIZATIONS...
C...
DO 480 I=1,NCNR
  LABLFF(I) = 0
  LABLFP(I) = 0
  FCOST(I) = 99.9
480 CONTINUE
C
JFORWD = NODEST
LABLFF(JFORWD) = 1
FCOST(JFORWD) = 0.
C...
DO 540 I=1,6
  NEXT = NETGRD(JFORWD,I)
  IF (NEXT.EQ.0) GO TO 540
  IF (LABLFF(NEXT).EQ.1) GO TO 540
520 CALL SEGOPT (JFORWD,NEXT,SUVCOS,RADVN)
530 TCOST = SUVCOS + FCOST(JFORWD)
  IF (TCOST.GT.FCOST(NEXT)) GO TO 540
  FCOST(NEXT) = TCOST
  LABLFP(NEXT) = JFORWD
  OFTSPD(NEXT) = RADVN
540 CONTINUE
  COSTMN = 99.9
C...
DO 560 J=1,NCVR
  IF (LABLFP(J).EQ.0) GO TO 560
  IF (LABLFF(J).EQ.1) GO TO 560

```

```

RUT01350
RUT01360
RUT01370
RUT01380
RUT01390
RUT01400
RUT01410
RUT01420
RUT01430
RUT01440
RUT01450
RUT01460
RUT01470
RUT01480
RUT01490
RUT01500
RUT01510
RUT01520
RUT01530
RUT01540
RUT01550
RUT01560
RUT01570
RUT01580
RUT01590
RUT01600
RUT01610
RUT01620
RUT01630
RUT01640
RUT01650
RUT01660
RUT01670
RUT01680
RUT01690
RUT01700
RUT01710
RUT01720
RUT01730
RUT01740
RUT01750
RUT01760
RUT01770
RUT01780
RUT01790
RUT01800
RUT01810
RUT01820

```

```

IF (FCOST(J).GT.COSTMN) GO TO 560
COSTMN = FCOST(J)
JFORWD = J
560 CONTINUE
C...PREPARING FOR NEXT ITERATION...
LABLFF(JFORWD) = 1
IF (JFORWD.NE.NODSTR) GO TO 500
C
C...FROM NOW ON LABLFF(I) IS THE NODE NUMBERS IN THE SELECTED ROUTE...
600 I = 1
LABLFF(I) = NODSTR
620 I = I + 1
LABLFF(I) = LABLFF(LABLFF(I-1))
IF (LABLFF(I).NE.NODEST) GO TO 620
640 NSEGM = I
700 DO 720 K=1,NSEGM
LTEMP = LABLFF(K)
XROUTE(K) = TPOG(LTEMP,1)
YROUTE(K) = TPOG(LTEMP,2)
OPRADV(K) = OFTSPD(LTEMP)
720 CONTINUE
WRITE (14,6670) SEGMEN,SEGSIZ
6670 FORMAT (/,/, INPUT- AND WORKING-SEGMENT LENGTH : ',2F6.1)
730 WRITE (14,6650) NELATK
6650 FORMAT (/,/, NUMBER OF ATTACKING ELEMENTS : ',16)
735 WRITE (14,6645) XSTART,YSTART
6645 FORMAT (/,/, STARTING-POSITION IS ',2F10.1)
740 WRITE (14,6665) XDEST,YDEST
6665 FORMAT (/,/, DESTINATION-COORDS. : ',2F10.1)
745 WRITE (14,6655)
6655 FORMAT (/,/, DEF.D.UNITS, STRENGTH AND LOCATIONS : ')
DO 750 I=1,NLOC
750 WRITE (14,6660) I,XDEFDK(I),YDEFDK(I)
6660 FORMAT (/,/, I,NDEFDK(I),XDEFDK(I),YDEFDK(I),218,2F10.1)
CONTINUE
750 WRITE (14,6680) ASSR,RANGEM
6680 FORMAT (/,/, ASSAULT- AND MAX-WEAPON-RANGE(METERS) : ',2F8.1)
WRITE (14,6635)
DO 820 K=1,NSEGM
820 WRITE (14,6640) K,LABLFF(K),XROUTE(K),YROUTE(K),OPRADV(K)
CONTINUE
C

```

```

RUT01830
RUT01840
RUT01850
RUT01860
RUT01870
RUT01880
RUT01890
RUT01900
RUT01910
RUT01920
RUT01930
RUT01940
RUT01950
RUT01960
RUT01970
RUT01980
RUT01990
RUT02000
RUT02010
RUT02020
RUT02030
RUT02040
RUT02050
RUT02060
RUT02070
RUT02080
RUT02090
RUT02100
RUT02110
RUT02120
RUT02130
RUT02140
RUT02150
RUT02160
RUT02170
RUT02180
RUT02190
RUT02200
RUT02210
RUT02220
RUT02230
RUT02240

```

```

6590 FORMAT (//, '
6600 FORMAT (//, '
6605 FORMAT (//, '
6608 FORMAT (2111, 516)
6630 FORMAT (//, 'NEXT, JBACW, SUVCOS, RADVN ', 216, 2F12.6)
6635 FORMAT (//, '10X, 'K, NODE-NBR', XCOORD', 216, 2F12.1, F8.1)
6640 FORMAT (5X, 216, 2F12.1, F8.1)
9999 STOP
      END
C
C
      EXERCISE-#3, VARYING TWO D-UNIT'S STRENGTH..', /)
      DIST, ORIGIN W.R.T. TOPOG.MAP', 3F7.0)
      NTEMP, NCOL, NROW', 315)
      RUT02250
      RUT02260
      RUT02270
      RUT02280
      RUT02290
      RUT02300
      RUT02310
      RUT02320
      RUT02330
      RUT02340
      RUT02350

```

```

SUBROUTINE SEGOPT(NODNOM, NODNXT, SVCOST, RATVNC)
DIMENSION MAPINF(6,20,20), MAPCON(20,20), MAPRSP(20,20), PKFOE(28,40)
DIMENSION COSTGD(925,6), TOPOG(925,2), LABLFF(925), LABLFP(925),
DIMENSION NETGRD(925,6), XROUTE(925), YROUTE(925), OPRADV(925),
*FCOST(925), OFISPD(925), YDEFDK(6), NDEFDK(6), MIRROR(6)
DIMENSION XDEFDK(28), PKVOE(28)
DIMENSION MAPINF, MAPCON, MAPRSP, PKFOE, TOPOG, XDEFDK, YDEFDK, NDEFDK
COMMON FCYCLE, PIXLE, PKVL, RRANGE, SEGR3, SEGSIZ, NCCL, NELATK, NLOC,
*XWEST, YEAST, YNORTH, YSOUTH, NCOLHX, NCL, SEGCYC

C...ONE SEGMENT IS REPRESENTED BY THREE POINTS : 'NOW', 'MID' AND 'NXT'...
XNOW = TOPOG(NODNOM,1)
YNOW = TOPOG(NODNOM,2)
XNXT = TOPOG(NODNXT,1)
YNXT = TOPOG(NODNXT,2)
XMID = (XNOW+XNXT)/2.
YMID = (YNOW+YNXT)/2.
INOW = 1 + (YNORTH-YNOW)/PIXLE
JMID = 1 + (YNORTH-YMID)/PIXLE
JNXT = 1 + (YNORTH-YNXT)/PIXLE
JNXT = 1 + (XNXT-XWEST)/PIXLE
*JNXT)/3.
C...COMPONENT OF PKILL DUE TO TERRAIN...
IF (MAPRSP(INOW, JNOW).EQ.0) GO TO 210
IF (MAPRSP(JMID, JNXT).EQ.0) GO TO 210
IF (MAPRSP(JNXT, JNXT).EQ.0) GO TO 210
ADVEL=(MAPRSP(INOW, JNOW)+MAPRSP(JMID, JNXT)+MAPRSP(JNXT, JNXT))/3.
JADV = (ADVEL + .5)
GO TO 220
210 SVCOST = 99.9
RATVNC = 0.
RETURN
220 DO 260 J=JADV,27
V=J
PKVEL(J) = PKVL * (V/ADVEL)**3
260 CONTINUE
C...PKILL COMPONENT DUE TO DEFENDING UNIT...
DO 270 J=JADV,27
PKVOE(J) = 0.
270 CONTINUE
C... DO 300 I=1, NLJC
C...TEST IF THE I-TH DEFEND UNIT IS IN THE VICINITY OF THE DESTINATION...
IF ((XDEFDK(I)-XDEST)**2+(YDEFDK(I)-YDEST)**2).LT.ASSRR)GO TO 300

```

```

RUT02360
RUT02370
RUT02380
RUT02390
RUT02400
RUT02410
RUT02420
RUT02430
RUT02440
RUT02450
RUT02460
RUT02470
RUT02480
RUT02490
RUT02500
RUT02510
RUT02520
RUT02530
RUT02540
RUT02550
RUT02560
RUT02570
RUT02580
RUT02590
RUT02600
RUT02610
RUT02620
RUT02630
RUT02640
RUT02650
RUT02660
RUT02670
RUT02680
RUT02690
RUT02700
RUT02710
RUT02720
RUT02730
RUT02740
RUT02750
RUT02760
RUT02770
RUT02780
RUT02790
RUT02800
RUT02810
RUT02820
RUT02830

```



```

C...:TEST IF THE I-TH DEF.D.U.NIT INFLUENCES THE CURRENT SEGMENT...
C...:INFL=MAPINF(I,INOW,JNOW)+MAPINF(I,IMID,JMID)+MAPINF(I,INXT,
C...: *JNXT)
C...:IF (INFL.LT.2) GO TO 300
C...:TEST IF THIS SEGMENT IS WITHIN RANGE OF I-TH DEF.D.U.NIT...
C...:DISQR = (XDEFK(I)-XMID)**2 + (YDEFK(I)-YMID)**2
C...:IF (DISQR.GT.RRANGE) GO TO 300
C...:DIST = SQRT(DISQR)
C...:IDIST = (1 + DIST/PIXLE)
C...:DETERMINE (ASPECT-)ANGLE-FACTOR...
C...:DISQR = (XDEFK(I)-XNOW)**2 + (YDEFK(I)-YNOW)**2
C...:ANGLFC = 1.
C...:IF (DISQR.GT.(SEGSIZ**2/4. + DISQR + DISQR*SEGR3/4.)) ANGLFC=3.
C...:CONCEALMENT FACTOR...
C...:OPNFC=(MAPCON(INOW,JNOW)+MAPCON(IMID,JMID)+MAPCON(INXT,
C...: *JNXT))/30.
C...:COMPUTE PKILL DUE TO DEFENDER FOR VARIOUS ADVANCING RATE...
C...:DO 280 J=JADV,27
C...:PKVOE(J) = PKVOE(J)+PKFOE(J,IDIST)*OPNFC*ANGLFC*NDEFK(I)/NELATK
C...:280 CONTINUE
C...:300 CONTINUE
C...:LOOKING FOR OPTIMUM SPEED FOR WHICH MIN. TOTAL PKILL OCCURS...
C...:320 SVCOST = 1.
C...:DO 400 J=JADV,27
C...:PKTOT = SEGSIZ * (PKVOE(J)/(FCYCLE*J) + PKVEL(J)/1609)
C...:IF (PKTOT.GT.SVCOST) GO TO 400
C...:SVCOST = PKTOT
C...:RATVNC = J
C...:400 CONTINUE
C...:RETURN
C...:END
C
C
C SUBROUTINE NNKFOG(SGRT3,SGSIZ,NCLHX,NCCCL,NODN,XORT,YORT)
C TRANSFORMING NODE-NUMBER INTO THE ORTHOGONAL-COORDINATE-SYSTEM OF THE
C ROUTE-SELECTION-MAP....
C NHX=(NODN/NCCCL)
C IXESS=NODN-(NHX*NCCCL)
C YORT=NHX*SGRT3
C IF (IXESS.GT.0) GO TO 40

```

RUT02840
 RUT02850
 RUT02860
 RUT02870
 RUT02880
 RUT02890
 RUT02900
 RUT02910
 RUT02920
 RUT02930
 RUT02940
 RUT02950
 RUT02960
 RUT02970
 RUT02980
 RUT02990
 RUT03000
 RUT03010
 RUT03020
 RUT03030
 RUT03040
 RUT03050
 RUT03060
 RUT03070
 RUT03080
 RUT03090
 RUT03100
 RUT03110
 RUT03120
 RUT03130
 RUT03140
 RUT03150
 RUT03160
 RUT03170
 RUT03180
 RUT03190
 RUT03200
 RUT03210
 RUT03220
 RUT03230
 RUT03240
 RUT03250
 RUT03260
 RUT03270
 RUT03280
 RUT03290

```

XORT=(NCLHX-1.5)*SGSIZ
YORT=YORT-.5*SGRT3
RETURN
40 IF (IXESS.GT.NCLHX) GO TO 80
XORT=(IXESS-1.)*SGSIZ
RETURN
80 XORT=(IXESS-NCLHX-.5)*SGSIZ
YORT=YORT+.5*SGRT3
RETURN
END

C..
SUBROUTINE OGXFNN(XORT,YORT,NODN)
COMMON MAPINF,MAPCON,MAPRSP,PKFOE,TOPOG,XDEFDK,YDEFDK,NDEFDK
COMMON FCYCLE,PIXLE,PKVL,RRANGE,SEGR3,SEGSIZ,NCCI,NELATK,NLOC,
*XWEST,XEAST,YNORTH,YSOUTH,NCOLHX,NCL,SEGCYC
NHX=(YORT*2./SEGR3+.5)
NHH=(NHX/2)
IXESS=NHX-2*NHH
MHX=((XORT/SEGSIZ)+(2.-IXESS)/2.)
NODN=(NHH*NCCI+IXESS*NCL+MHX)
RETURN
END

C
SUBROUTINE RSTRTP(XTRANS,YTRANS,SINR,COSR,XRS,YRS,XTOP,YTOP)
XTRANS AND YTRANS ARE THE COORD. OF ORIGIN IN RS-MAP W.R.T. TOPG.-MAP.
SINR AND COSR ARE SINE AND COSINE OF THE ANGLE-OF-ROTATION OF RS-MAP.
XTOP = XRS*COSR - YRS*SINR + XTRANS
YTOP = XRS*SINR + YRS*COSR + YTRANS
RETURN
END

C
SUBROUTINE IPTRRS(XTRANS,YTRANS,SINR,COSR,XTOP,YTOP,XRS,YRS)
TO TRANSFORM TOPOGR.-MAP-COORDS. INTO ROUTE-SELECT.-MAP COORD.....
(TRANSF. WITH BOTH TRANS
XTEMP = XTOP - YTRANS
YTEMP = YTOP + XTRANS
XRS = XTEMP*COSR + YTEMP*SINR
YRS = -XTEMP*SINR + YTEMP*COSR
RETURN
END

C...

```

RUT03300
RUT03310
RUT03320
RUT03330
RUT03340
RUT03350
RUT03360
RUT03370
RUT03380
RUT03390
RUT03400
RUT03410
RUT03420
RUT03430
RUT03440
RUT03450
RUT03460
RUT03470
RUT03480
RUT03490
RUT03500
RUT03510
RUT03520
RUT03530
RUT03540
RUT03550
RUT03560
RUT03570
RUT03580
RUT03590
RUT03600
RUT03610
RUT03620
RUT03630
RUT03640
RUT03650
RUT03660
RUT03670
RUT03680
RUT03690
RUT03700
RUT03710
RUT03720

104

**** INPUT DATA FOR EXERCISING THE ROUTE-SELECTION ROUTINE ****

4000.	6000.	7500.	5500.	140.	20.
2					
4233.	4937.				
6691.	6362.				
0603.					
4310.	7237.				
5535.	5670.				
100.	4000.	500.	.0002		
0036					
898889886431011785432					
789988997531012785453					
56879985641013885310					
4458989761112784200					
3469898651226987541					
245988988753347876401					
335499988995768975331					
113449975898998765453					
25458988789899874532					
54589897678989985312					
56788975656579988410					
67899964357998997521					
57989875468899897543					
6888987878998987654					
57759899998769989653					
4568899998626898641					
46589999997525687531					
35699999898614798530					
245998999899525897522					
116799989998626755434					
1314151514131211266					
1211112114131211265					
111111121314131194					
1111212141512978000					
1121131313121331401					
1111101111112131101					
1111910101211291211					
10111213108109107					
1111211131112118					
64334670004121151311					
3232591211514121311					
4661011111111108					
6810111111111108					
4661011111111108					
91012129					
979977877867996					
56955779964					

106

[illegible]

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0-03420 0-03020 0-02665 0-02764 0-02665 0-02352 0-02075 0-01832 0-01616 0-01426 0-01259 0-01118
0-00980 0-00865 0-00764 0-00764 0-00764 0-00674 0-00595 0-00525 0-00463 0-00409 0-00361 0-00318
0-00281 0-00248 0-00219 0-00219 0-00219 0-00193 0-00170 0-00150 0-00133 0-00117 0-00103 0-00091
0-00988 0-00902 0-00858 0-00858 0-00858 0-00752 0-00665 0-00582 0-00519 0-00458 0-00402 0-00356
0-00902 0-00796 0-00728 0-00728 0-00728 0-00620 0-00547 0-00483 0-00426 0-00376 0-00332 0-00293
0-00258 0-00228 0-00228 0-00228 0-00228 0-00178 0-00157 0-00138 0-00122 0-00108 0-00095 0-00084
0-00110 0-00097 0-00097 0-00097 0-00097 0-00091 0-00077 0-00069 0-00066 0-00066 0-00066 0-00066
0-00830 0-00732 0-00732 0-00732 0-00732 0-00691 0-00646 0-00611 0-00580 0-00546 0-00512 0-00482
0-00238 0-00210 0-00210 0-00210 0-00210 0-00163 0-00144 0-00127 0-00112 0-00099 0-00087 0-00077
0-09301 0-08209 0-08209 0-08209 0-08209 0-06393 0-05642 0-04979 0-04394 0-03877 0-03422 0-03020
0-02665 0-02352 0-02352 0-02352 0-02352 0-01832 0-01616 0-01426 0-01259 0-01118 0-00980 0-00865
0-00764 0-00674 0-00674 0-00674 0-00674 0-00525 0-00463 0-00409 0-00361 0-00318 0-00281 0-00248
0-00219 0-00193 0-00193 0-00193 0-00193 0-00150 0-00133 0-00117 0-00103 0-00091 0-00084 0-00077

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*** END DATA ***

APPENDIX D: RESULTS OF MODEL EXERCISE

Computer printouts presented in this appendix show the results of the exercises conducted with the route selection model. Some of the output variables are self explanatory; the others are explained below in the order of occurrence.

- DIST - Distance from the starting point to the destination. In the exercises, it was in meters.
- ORIGIN ... - (With respect to Topographic Map), is a pair of coordinates showing the location of the R-S-Map's origin with respect to the Topographic Map's origin. These coordinates also designate the location of node #1 of the network grid.
- NTEMP - Network grid size parameter, determined by distance and segment length. See also Nomenclature in Fig. IV-4.
- SEGMENT LENGTH - The length of each segment in the route. The routine except the input segment length; then for standardization purpose of the network grid, the input segment length is adjusted to become working segment length.
- DEFD.UNITS - Defending units under consideration

STRENGTH	- Number of known elements in the particular (unit) location. STRENGTH = 0 means that no defending unit is known to be in that location.
ASSAULT RANGE	- Range in which "close-in" combat is considered to occur. It is characterized by the situation where nobody cares anymore about selection of route.
K	- Segment number in the selected route
NODE NBR	- Node number of Network grid which is the "working-map" of the Dijkstra Algorithm.
X, YCOORD	- The abscissa and ordinate of the location of the corresponding node mentioned in NODE NBR.
CPT.R.O.ADV	- Optimum rate of Advance, found by the route selection routine for each segment of the route.

APPENDIX - D-1.

EXERCISE-#1, MANIPULATION OF COORDINATES....

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4789. 7934.

NTEMP,NCCL,NROW 9 14 27

INPUT- AND WORKING-SEGMENT LENGTH : 120.0 120.8

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFD.UNITS, STRENGTH AND LOCATIONS :

1	0	4233.0	6691.0
2	0	4537.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	CPT.R.O.ADV.
1	48	4310.0	7237.0	14.0
2	61	4418.3	7183.5	13.0
3	74	4526.6	7129.9	13.0
4	88	4534.4	7009.3	11.0
5	101	4642.7	6955.8	8.0
6	115	4650.5	6835.2	12.0
7	129	4658.3	6714.7	11.0
8	143	4666.1	6594.1	12.0
9	156	4774.4	6540.6	12.0
10	170	4782.2	6420.0	11.0
11	183	4890.6	6366.4	9.0
12	196	4998.9	6312.9	12.0
13	209	5107.2	6259.4	14.0
14	223	5115.0	6138.8	14.0
15	237	5122.8	6018.2	10.0
16	251	5130.6	5897.6	8.0
17	264	5238.9	5844.1	8.0
18	278	5246.7	5723.5	9.0
19	291	5355.0	5670.0	0.0

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APPENDIX - D-2.

EXERCISE-#1, MANIPULATION OF COORDINATES....

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4876. 4973.

NTEMP,NCCL,NROW 9 14 27

INPUT- AND WORKING-SEGMENT LENGTH : 120.0 120.8

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 5355.0 5670.0

DESTINATION-COORDS. : 4310.0 7237.0

DEFD.UNITS, STRENGTH AND LOCATIONS :

1	0	4233.0	6691.0
2	0	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	48	5355.0	5670.0	9.0
2	61	5246.7	5723.5	8.0
3	75	5238.9	5844.1	8.0
4	88	5130.6	5897.6	10.0
5	102	5122.8	6018.2	14.0
6	116	5115.0	6138.8	14.0
7	130	5107.2	6259.4	12.0
8	143	4998.9	6312.9	9.0
9	156	4890.6	6366.4	11.0
10	169	4782.2	6420.0	12.0
11	183	4774.4	6540.6	12.0
12	196	4666.1	6594.1	11.0
13	210	4658.3	6714.7	12.0
14	224	4650.5	6835.2	8.0
15	238	4642.7	6955.8	11.0
16	251	4534.4	7009.3	13.0
17	265	4526.6	7129.9	13.0
18	278	4418.3	7183.5	14.0
19	291	4310.0	7237.0	0.0

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APPENDIX - D-3.

EXERCISE-#1, MANIPULATION OF COORDINATES....

DIST,ORIGIN W.R.T. TOPOG.MAP 1878. 6571. 6701.

NTEMP,NCCL,NROW 9 14 27

INPUT- AND WORKING-SEGMENT LENGTH : 120.0 120.5

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 5870.0 7170.0

DESTINATION-COORDS. : 4320.0 6109.0

CEFD.UNITS, STRENGTH AND LOCATIONS :

1	0	4233.0	6691.0
2	0	4537.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	48	5870.0	7170.0	8.0
2	62	5749.9	7160.8	12.0
3	76	5629.7	7151.5	11.0
4	90	5509.6	7142.3	11.0
5	104	5389.4	7133.1	9.0
6	118	5269.3	7123.9	5.0
7	132	5149.1	7114.6	4.0
8	145	5097.1	7006.0	6.0
9	159	4976.9	6996.7	7.0
10	173	4856.8	6987.5	7.0
11	187	4736.6	6978.3	7.0
12	200	4684.6	6869.6	10.0
13	213	4632.5	6761.0	13.0
14	226	4580.4	6652.3	11.0
15	239	4528.3	6543.6	11.0
16	252	4476.2	6435.0	10.0
17	265	4424.2	6326.3	12.0
18	278	4372.1	6217.7	14.0
19	291	4320.0	6109.0	0.0

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APPENDIX - D-4.

EXERCISE-#1, MANIPULATION OF COORDINATES....

DIST,ORIGIN W.R.T. TOPOG.MAP 1550. 6202. 6459.

NTEMP,NCCL,NROW 7 12 23

INPUT- AND WORKING-SEGMENT LENGTH : 120.0 127.8

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 5870.0 7161.95

DESTINATION-COORDS. : 4320.0 7161.92

DEFD.UNITS, STRENGTH AND LOCATIONS :

1	0	4233.0	6691.0
2	0	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	41	5870.0	7161.9	8.0
2	53	5759.3	7225.9	9.0
3	65	5648.6	7289.8	9.0
4	77	5537.8	7353.7	9.0
5	89	5427.1	7417.6	8.0
6	100	5316.4	7353.7	6.0
7	112	5205.7	7417.6	3.0
8	123	5095.0	7353.7	4.0
9	134	4984.3	7289.8	7.0
10	145	4873.6	7225.9	11.0
11	157	4762.9	7289.8	13.0
12	169	4652.1	7353.7	15.0
13	180	4541.4	7289.8	15.0
14	191	4430.7	7225.8	13.0
15	202	4320.0	7161.9	0.0

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APPENDIX - D-5.

EXERCISE-#2, VARIATIONS IN SEGMENT-LENGTHS...

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4692. 8624.
 NTEMP,NCOL,NROW 4 9 17
 INPUT- AND WORKING-SEGMENT LENGTH : 240.0 271.9
 NUMBER OF ATTACKING ELEMENTS : 36
 STARTING-POSITION IS 4310.0 7237.0
 DESTINATION-COORDS. : 5355.0 5670.0
 DEFD.UNITS, STRENGTH AND LCCATIONS :
 1 0 4233.0 6691.0
 2 0 4937.0 6362.0
 ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	39	4310.0	7237.0	13.0
2	48	4327.5	6965.7	13.0
3	56	4571.2	6845.2	11.0
4	65	4588.8	6574.0	11.0
5	74	4606.3	6302.7	8.0
6	82	4850.0	6182.2	10.0
7	91	4867.6	5910.9	9.0
8	99	5111.3	5790.5	8.0
9	107	5355.0	5670.0	0.0

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APPENDIX - D-6.

EXERCISE-#2, VARIATIONS IN SEGMENT-LENGTHS...

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4716. 8262.

NTEMP,NCGL,NROW 6 11 21

INPUT- AND WORKING-SEGMENT LENGTH : 160.0 181.2

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFD.UNITS, STRENGTH AND LOCATIONS :

1	0	4233.0	6691.0
2	0	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	48	4310.0	7237.0	13.0
2	58	4472.5	7156.7	14.0
3	69	4484.2	6975.8	13.0
4	80	4495.9	6795.0	13.0
5	90	4658.3	6714.7	11.0
6	100	4820.8	6634.4	10.0
7	111	4832.5	6453.5	9.0
8	122	4844.2	6272.6	8.0
9	133	4855.9	6091.8	11.0
10	144	4867.6	5910.9	10.0
11	154	5030.0	5830.6	7.0
12	164	5192.5	5750.3	8.0
13	174	5355.0	5670.0	0.0

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APPENDIX - D-7.

EXERCISE-#2, VARIATIONS IN SEGMENT-LENGTHS...

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4789. 7934.

NTEMP,NCOL,NROW 9 14 27

INPUT- AND WORKING-SEGMENT LENGTH : 120.0 120.8

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFO.UNITS, STRENGTH AND LCCATIONS :

1	0	4233.0	6691.0
2	0	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	48	4310.0	7237.0	14.0
2	61	4418.3	7183.5	13.0
3	74	4526.6	7129.9	13.0
4	88	4534.4	7009.3	11.0
5	101	4642.7	6955.8	8.0
6	115	4650.5	6835.2	12.0
7	129	4658.3	6714.7	11.0
8	143	4666.1	6594.1	12.0
9	156	4774.4	6540.6	12.0
10	170	4782.2	6420.0	11.0
11	183	4890.6	6366.4	9.0
12	196	4998.9	6312.9	12.0
13	209	5107.2	6259.4	14.0
14	223	5115.0	6138.8	14.0
15	237	5122.8	6018.2	10.0
16	251	5130.6	5897.6	8.0
17	264	5238.9	5844.1	8.0
18	278	5246.7	5723.5	9.0
19	291	5355.0	5670.0	0.0

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APPENDIX - D-8.

EXERCISE-#2, VARIATIONS IN SEGMENT-LENGTHS...

DIST, ORIGIN W.R.T. TOPOG. MAP 1883. 4781. 7812.
 NTEMP, NCOL, NROW 13 18 35
 INPUT- AND WORKING-SEGMENT LENGTH : 80.0 83.6
 NUMBER OF ATTACKING ELEMENTS : 36
 STARTING-POSITION IS 4310.0 7237.0
 DESTINATION-COORDS. : 5355.0 5670.0
 DEFD. UNITS, STRENGTH AND LOCATIONS :
 1 0 4233.0 6691.0
 2 0 4937.0 6362.0
 ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ACV.
1	62	4310.0	7237.0	13.0
2	80	4315.4	7153.5	12.0
3	98	4320.8	7070.1	13.0
4	116	4326.2	6986.6	14.0
5	133	4401.2	6949.5	14.0
6	151	4406.6	6866.0	12.0
7	169	4412.0	6782.6	12.0
8	187	4417.4	6699.1	11.0
9	204	4492.3	6662.0	11.0
10	222	4497.7	6578.6	11.0
11	239	4572.7	6541.5	10.0
12	256	4647.7	6504.4	9.0
13	274	4653.1	6420.9	9.0
14	291	4728.1	6383.9	9.0
15	308	4803.1	6346.8	10.0
16	325	4878.1	6309.8	9.0
17	342	4953.1	6272.7	9.0
18	360	4958.5	6189.2	10.0
19	378	4963.9	6105.7	11.0
20	396	4969.3	6022.3	11.0
21	413	5044.2	5985.2	8.0
22	430	5119.2	5948.1	7.0
23	448	5124.6	5864.7	8.0
24	465	5199.6	5827.6	8.0
25	482	5274.6	5790.5	9.0
26	499	5349.6	5753.5	10.0
27	517	5355.0	5670.0	0.0

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APPENDIX - D-9.

EXERCISE-#3, VARYING ONE DEFEND. UNIT'S STRENGTH...

DIST, ORIGIN W.R.T. TOPOG. MAP 1883. 4757. 8047.
 NTEMP, NCOL, NROW 7 12 23
 INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3
 NUMBER OF ATTACKING ELEMENTS : 36
 STARTING-POSITION IS 4310.0 7237.0
 DESTINATION-COORDS. : 5355.0 5670.0
 DEFEND. UNITS, STRENGTH AND LOCATIONS :
 1 0 4233.0 6691.0
 2 0 4937.0 6362.0
 ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ACV.
1	41	4310.0	7237.0	13.0
2	53	4320.0	7082.0	13.0
3	64	4459.3	7013.1	13.0
4	75	4598.5	6944.3	11.0
5	87	4608.6	6789.3	12.0
6	98	4747.8	6720.4	11.0
7	110	4757.9	6565.4	12.0
8	122	4767.9	6410.4	10.0
9	133	4907.1	6341.6	9.0
10	145	4917.2	6186.5	10.0
11	156	5056.4	6117.7	13.0
12	167	5195.7	6048.9	10.0
13	179	5205.7	5893.9	8.0
14	190	5345.0	5825.0	10.0
15	202	5355.0	5670.0	0.0

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APPENDIX - D-10.

EXERCISE-#3, VARYING ONE DEF.D.UNIT'S STRENGTH...

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4797. 8047.

NTEMP,NCCL,NROW 7 12 23

INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEF.D.UNITS, STRENGTH AND LOCATIONS :

1	2	4233.0	6691.0
2	0	4537.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	41	4310.0	7237.0	27.0
2	52	4449.3	7168.2	27.0
3	64	4459.3	7013.1	27.0
4	75	4598.5	6944.3	27.0
5	87	4608.6	6789.3	27.0
6	98	4747.8	6720.4	27.0
7	110	4757.9	6565.4	27.0
8	122	4767.9	6410.4	10.0
9	133	4907.1	6341.6	9.0
10	145	4917.2	6186.5	10.0
11	156	5056.4	6117.7	13.0
12	167	5195.7	6048.9	10.0
13	179	5205.7	5893.9	8.0
14	190	5345.0	5825.0	10.0
15	202	5355.0	5670.0	0.0

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APPENDIX - D-11.

EXERCISE-#3, VARYING ONE DEFEND. UNIT'S STRENGTH...

DIST, ORIGIN W.R.T. TOPOG. MAP 1883. 4797. 8047.

NTEMP, NCOL, NROW 7 12 23

INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFEND. UNITS, STRENGTH AND LOCATIONS :

1	4	4233.0	6691.0
2	0	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	41	4310.0	7237.0	27.0
2	40	4439.2	7323.2	27.0
3	39	4568.5	7409.4	27.0
4	38	4697.7	7495.6	27.0
5	49	4837.0	7426.7	23.0
6	60	4976.3	7357.9	15.0
7	59	5105.5	7444.1	9.0
8	70	5244.8	7375.3	6.0
9	82	5254.8	7220.2	18.0
10	94	5264.8	7065.2	27.0
11	106	5274.8	6910.2	27.0
12	118	5284.8	6755.2	27.0
13	130	5294.9	6600.1	27.0
14	131	5165.6	6513.9	14.0
15	143	5175.6	6358.9	15.0
16	155	5185.7	6203.9	14.0
17	167	5195.7	6048.9	10.0
18	179	5205.7	5893.9	8.0
19	190	5345.0	5825.0	10.0
20	202	5355.0	5670.0	0.0

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APPENDIX - D-12.

EXERCISE-#3, VARYING ONE DEFD.UNIT'S STRENGTH...

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4797. 8047.
 NTEMP,NCCL,NRCW 7 12 23
 INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3
 NUMBER OF ATTACKING ELEMENTS : 36
 STARTING-POSITION IS 4310.0 7237.0
 DESTINATION-CCORDS. : 5355.0 5670.0
 DEF.D.UNITS, STRENGTH AND LCCATIONS :
 1 8 4233.0 6691.0
 2 0 4937.0 6362.0
 ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ACV.
1	41	4310.0	7237.0	27.0
2	40	4439.2	7323.2	27.0
3	39	4568.5	7409.4	27.0
4	38	4697.7	7495.6	27.0
5	49	4837.0	7426.7	26.0
6	60	4976.3	7357.9	17.0
7	59	5105.5	7444.1	10.0
8	70	5244.8	7375.3	6.0
9	82	5254.8	7220.2	21.0
10	94	5264.8	7065.2	27.0
11	106	5274.8	6910.2	27.0
12	118	5284.8	6755.2	27.0
13	130	5294.9	6600.1	27.0
14	131	5165.6	6513.9	14.0
15	142	5175.6	6358.9	15.0
16	155	5185.7	6203.9	14.0
17	167	5195.7	6048.9	10.0
18	179	5205.7	5893.9	8.0
19	190	5345.0	5825.0	10.0
20	202	5355.0	5670.0	0.0

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APPENDIX - D-13.

EXERCISE-#4, VARYING TWO DEFD.UNIT'S STRENGTH...

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4797. 8047.

NTEMP,NCCL,NROW 7 12 23

INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFD.UNITS, STRENGTH AND LCCATIONS :

1	0	4233.0	6691.0
2	1	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	41	4310.0	7237.0	25.0
2	42	4180.7	7150.8	22.0
3	43	4051.5	7064.6	13.0
4	55	4061.5	6909.6	12.0
5	67	4071.6	6754.6	10.0
6	79	4081.6	6599.5	9.0
7	90	4220.8	6530.7	11.0
8	102	4230.9	6375.7	11.0
9	114	4240.9	6220.7	13.0
10	125	4380.1	6151.8	14.0
11	136	4519.4	6083.0	16.0
12	148	4529.4	5928.0	15.0
13	159	4668.7	5859.1	13.0
14	170	4808.0	5790.3	27.0
15	181	4947.2	5721.5	6.0
16	192	5086.5	5652.6	5.0
17	203	5225.7	5583.8	8.0
18	202	5355.0	5670.0	0.0

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APPENDIX - D-14.

EXERCISE-#4. VARYING TWO DEFEND. UNIT'S STRENGTH...

DIST, ORIGIN W.R.T. TOPOG. MAP 1883. 4797. 8047.

NTMP, NCCL, NROW 7 12 23

INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFEND. UNITS, STRENGTH AND LOCATIONS :

1	0	4233.0	6691.0
2	2	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	41	4310.0	7237.0	27.0
2	42	4180.7	7150.8	25.0
3	43	4051.5	7064.6	13.0
4	55	4061.5	6909.6	12.0
5	67	4071.6	6754.6	10.0
6	79	4081.6	6599.5	9.0
7	90	4220.8	6530.7	11.0
8	102	4230.9	6375.7	11.0
9	114	4240.9	6220.7	13.0
10	125	4380.1	6151.8	14.0
11	136	4519.4	6083.0	16.0
12	148	4529.4	5928.0	15.0
13	159	4668.7	5859.1	13.0
14	170	4808.0	5790.3	27.0
15	181	4947.2	5721.5	6.0
16	192	5086.5	5652.6	5.0
17	203	5225.7	5583.8	8.0
18	202	5355.0	5670.0	0.0

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APPENDIX - D-15.

EXERCISE-#4, VARYING TWO DEFEND. UNIT'S STRENGTH...

DIST, ORIGIN W.R.T. TOPOG. MAP 1883. 4757. 8047.

NTEMP, NCOL, NROW 7 12 23

INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFEND. UNITS, STRENGTH AND LOCATIONS :

1	2	4233.0	6691.0
2	2	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	41	4310.0	7237.0	27.0
2	42	4180.7	7150.8	27.0
3	43	4051.5	7064.6	27.0
4	55	4061.5	6909.6	27.0
5	67	4071.6	6754.6	27.0
6	79	4081.6	6599.5	27.0
7	91	4091.6	6444.5	27.0
8	103	4101.6	6289.5	27.0
9	114	4240.9	6220.7	27.0
10	125	4380.1	6151.8	27.0
11	136	4519.4	6083.0	27.0
12	147	4658.7	6014.2	27.0
13	158	4797.9	5945.3	27.0
14	169	4937.2	5876.5	27.0
15	180	5076.5	5807.7	8.0
16	191	5215.7	5738.8	9.0
17	202	5355.0	5670.0	0.0

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APPENDIX - D-16.

EXERCISE-#4, VARYING TWO DEFEND.UNIT'S STRENGTH...

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4797. 8047.

NTEMP,NCCL,NROW 7 12 23

INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFEND.UNIT'S, STRENGTH AND LOCATIONS :

1	4	4233.0	6691.0
2	2	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	41	4310.0	7237.0	27.0
2	42	4180.7	7150.8	27.0
3	43	4051.5	7064.6	27.0
4	55	4061.5	6909.6	27.0
5	67	4071.6	6754.6	27.0
6	78	4210.8	6685.7	27.0
7	89	4350.1	6616.9	27.0
8	100	4489.3	6548.1	27.0
9	111	4628.6	6479.2	27.0
10	122	4767.9	6410.4	10.0
11	133	4907.1	6341.6	27.0
12	144	5046.4	6272.7	27.0
13	155	5185.7	6203.9	27.0
14	167	5195.7	6048.9	27.0
15	179	5205.7	5893.9	20.0
16	191	5215.7	5738.8	9.0
17	202	5355.0	5670.0	0.0

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APPENDIX - D-17.

EXERCISE-#4, VARYING TWO DEF.D.UNIT'S STRENGTH...

DIST,ORIGIN W.R.T. TOPOG.MAP 1883. 4797. 8047.
 NTEMP,NCOL,NROW 7 12 23
 INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3
 NUMBER OF ATTACKING ELEMENTS : 36
 STARTING-POSITION IS 4310.0 7237.0
 DESTINATION-COORDS. : 5355.0 5670.0
 DEF.D.UNITS, STRENGTH AND LCCATIONS :
 1 8 4233.0 6691.0
 2 2 4937.0 6362.0
 ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	OPT.R.O.ACV.
1	41	4310.0	7237.0	27.0
2	42	4180.7	7150.8	27.0
3	43	4051.5	7064.6	27.0
4	55	4061.5	6909.6	27.0
5	67	4071.6	6754.6	27.0
6	78	4210.8	6685.7	27.0
7	89	4350.1	6616.9	27.0
8	100	4489.3	6548.1	27.0
9	111	4628.6	6479.2	27.0
10	122	4767.9	6410.4	10.0
11	133	4907.1	6341.6	27.0
12	144	5046.4	6272.7	27.0
13	155	5185.7	6203.9	27.0
14	167	5195.7	6048.9	27.0
15	179	5205.7	5893.9	20.0
16	191	5215.7	5738.8	9.0
17	202	5355.0	5670.0	0.0

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APPENDIX - D-18.

EXERCISE-#4, VARYING TWO DEF.D.UNIT'S STRENGTH...

DIST.ORIGIN W.R.T. TOPOG.MAP 1883. 4797. 8047.

NTEMP,NCCL,NROW 7 12 23

INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-POSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFD.UNITS, STRENGTH AND LOCATIONS :

1	12	4233.0	6691.0
2	2	4537.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	NODE-NBR	XCOORD	YCOORD	DPT.R.D.ADV.
1	41	4310.0	7237.0	27.0
2	40	4439.2	7323.2	27.0
3	39	4568.5	7409.4	27.0
4	38	4697.7	7495.6	27.0
5	49	4837.0	7426.7	27.0
6	60	4976.3	7357.9	19.0
7	59	5105.5	7444.1	11.0
8	70	5244.8	7375.3	6.0
9	82	5254.8	7220.2	22.0
10	94	5264.8	7065.2	27.0
11	106	5274.8	6910.2	27.0
12	118	5284.8	6755.2	27.0
13	130	5294.9	6600.1	27.0
14	142	5304.9	6445.1	27.0
15	154	5314.9	6290.1	27.0
16	166	5324.9	6135.1	27.0
17	167	5195.7	6048.9	27.0
18	179	5205.7	5893.9	20.0
19	191	5215.7	5738.8	9.0
20	202	5355.0	5670.0	0.0

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APPENDIX - D-19.

EXERCISE-#4, VARYING TWO DEFEND.UNIT'S STRENGTH...

DIST,ORIGIN W.R.T. TOPOG.MAP 1683. 4797. 8047.

NTEMP,NCCL,NROW 7 12 23

INPUT- AND WORKING-SEGMENT LENGTH : 140.0 155.3

NUMBER OF ATTACKING ELEMENTS : 36

STARTING-PCPOSITION IS 4310.0 7237.0

DESTINATION-COORDS. : 5355.0 5670.0

DEFEND.UNITS, STRENGTH AND LOCATIONS :

1	2	4233.0	6691.0
2	8	4937.0	6362.0

ASSAULT- AND MAX-WEAPON-RANGE(METERS) : 500.0 4000

K	MODE-NBR	XCOORD	YCOORD	OPT.R.O.ADV.
1	41	4310.0	7237.0	27.0
2	42	4180.7	7150.8	27.0
3	43	4051.5	7064.6	27.0
4	55	4061.5	6909.6	27.0
5	67	4071.6	6754.6	27.0
6	75	4081.6	6599.5	27.0
7	91	4091.6	6444.5	27.0
8	103	4101.6	6289.5	27.0
9	114	4240.9	6220.7	27.0
10	125	4380.1	6151.8	27.0
11	136	4519.4	6083.0	27.0
12	147	4658.7	6014.2	27.0
13	159	4668.7	5859.1	27.0
14	170	4808.0	5790.3	27.0
15	181	4947.2	5721.5	21.0
16	192	5086.5	5652.6	5.0
17	203	5225.7	5583.8	8.0
18	202	5355.0	5670.0	0.0

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